

## BIOMASS MODELING OF *ALNUS NEPALENSIS* D. DON AT JUVENILE STAGE

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### ABSTRACT

Juvenile stage plants contribute significant proportion of forest biomass and carbon depending on successional stage. Thus, the juvenile plants play a significant role in forest ecosystem and they cannot be neglected while estimating the total carbon stocks of the forest. Therefore this study was carried out develop juvenile biomass models. We measured diameter at 10 cm above ground level ( $D$ ), total height ( $H$ ) and total biomass ( $W$ ) of *Alnus nepalensis* juveniles. We used least square regression technique to develop biomass models. The models were estimated using “library(minpack.lm)” in R. The estimated models were evaluated by using numerical fit statistics and graphical analyses. Among 136 different models tested, the model of the form:  $W_i = \beta_0 + \beta_1(D2H)$  with explanatory variable  $D2H$  accounted for the largest proportion of biomass variations ( $R^2_{adj} = 0.97$ ;  $RMSE = 42.34g$ ;  $AIC = 406.8.7$ ) for individual *Alnus nepalensis* juveniles, and showed relatively better graphical appearance and biological logic.

**KEYWORDS:** *Alnus nepalensis*, Biomass model, juvenile stage

### INTRODUCTION

One or several predictor variables can generally be used to prepare biomass equations by using least square regression technique. Diameter, total height and wood density are the most widely used predictor variables, and these variables are used as a single or in combination with each other in the model (e.g. Chapa-gain et al., 2014; Chaturvedi et al., 2012; Subedi and Sharma, 2012; Basuki et al., 2009; Chave et al., 2005; Brown et al., 1989). Diameter is the easily and directly measurable variable therefore usually preferred for biomass modelling in spite of prediction accuracy of the developed models. The other variables are less frequently used in biomass modeling as they are difficult to measure in comparison to diameter (e.g. Kuyah et al., 2012; Ajit et al., 2011; Sharma, 2011; Singh et al., 2011; Telfer, 1969). Wood density may be considered as the best predictor variable as represents dry biomass or carbon amounts per unit volume of live wood and mechanical properties of plants (Navar, 2009a; Williamson & Wiemann, 2010). To better describe the variation of biomass across geographical areas due to difference in site qualities, stand structures, and species composition, wood density is incorporated into biomass models (e.g. Alvarez et al., 2012; Baker et al.,

2004; Basuki et al., 2009; Chaturvedi et al., 2010; Chaturvedi et al., 2012; Chave et al., 2005; Lindner and Sattler 2012; Nelson et al., 1999). However, because of the difficulties of getting information for this variable, biomass models with diameter alone or both diameter and height as explanatory variables are used. In this study only diameter and total height were used to develop bark biomass model.

Direct and indirect method can be used to estimate the individual tree and/or stand biomass. Cutting of plants and weighing of their parts to estimate biomass (direct method) is doubtlessly the most accurate method but it is very costly, time consuming and labor intensive (De Gier, 2003) and therefore it is commonly restricted to small areas and small sample size (Ketterings et al., 2001). The direct method is commonly used to validate the results of other less invasive and costly methods, such as estimation of biomass stock using non-invasive in-situ measurement and remote sensing (Clark et al., 2001). Allometric equations (Huxley & Teissier, 1936), yield the non-destructive and indirect estimate of biomass, are widely used for trees and forest biomass estimation (e.g. Chaturvedi et al., 2012; Subedi & Sharma, 2012; Sharma, 2011; Hosoda & Iehara, 2010). Morphometric variables such as plant diameter, height and density can easily be linked with dry matter content of the whole plant or its components via allometric equations (e.g. Subedi & Sharma, 2012; Ajit et al., 2011; Basuki et al., 2009; Ketterings et al., 2001; Navar, 2009a).

A number of studies (e.g. Brown et al., 1989; Singh & Singh, 1991; Ter-Mikaelian & Korzukhin, 1997; Keith et al., 2000; Segura & Kanninen, 2005; Zianis et al., 2005; Muukkonen, 2007; Navar, 2009b) have already indicated that the most of the studies on biomass have been undertaken on large sized forest species. A very limited biomass studies (e.g. Wagner & Ter-Mikaelian, 1999; Geudens et al., 2004; Chaturvedi & Raghubanshi, 2013; Chaturvedi et al., 2012; Chapagain et al., 2014) have been carried out for sapling and seedling hereafter termed as juveniles (defined as a plant  $\geq 30$  cm in height and  $< 10$  cm in stem circumference at 10 cm above ground surface (Chaturvedi et al., 2012). Depending on the successional stages of any of the forest stands, juveniles may contribute about 5% of the total share of forest biomass (Francis, 2000). Thus, the juvenile plants play a significant role in forest ecosystem and they cannot be neglected while estimating the total carbon stocks of the forest. Biomass estimation of juvenile stage plants is also indispensable in management of forest and research such as assessment of net primary productivity (Telfer, 1969; Hitchcock, 1978), carbon sequestration potential (Reed et al., 1995), living and dead understory forest fuels (Agee, 1983), fiber production potential (Hitchcock, 1978), and formulation of silvicultural guidelines for desired species (Ter-Mikaelian and Parker, 2000).

*Alnus nepalensis* D. Don (family Betulaceae), commonly known as Alder, is a pioneer, deciduous and gregarious tree species of middle hills of Nepal. It is commonly distributed from 500m to 2700 m elevation. Particularly, at lower elevations it is characteristic of moist sites such as near rivers and in ravines but it is also a colonist of scaly and gravelly land exposed by landslips, and of abandoned cultivation (Jackson, 1994). This species is commonly used for fuelwood though does not have a good calorific value. Although it is not considered to be the best

construction timber, it is very important in the middle hills for small timbers such as rafters, doors and window frames. It is also used for matches, papers and plywood (Jackson, 1994). The contribution of standing volumes of *Alnus nepalensis* to the total in the country has also been reported in DFRS (1999). Various natural and anthropogenic disturbances have been observed on the juvenile stage of forests in Nepal (Sapkota et al., 2009), but the intensity of disturbance is comparatively low in the study site due to community management regimes. A huge proportion of forest in the study site is in juvenile stage, and development of biomass models for them is very important from a biomass or carbon quantification point of view. A considerable underestimation of the total carbon in forest is realized due to unavailability of biomass model for juvenile stage plants. It is very essential to include juvenile stage plants in biomass studies because the role of juveniles in any forest is highly valuable from the carbon trade point of view. So far, to the authors' knowledge, no biomass studies have been conducted for juveniles of *Alnus nepalensis* in Nepal. Therefore, this work was carried out as a complementary work to reduce this gap, which led to the development of biomass models for the prediction of above-ground biomass for juveniles of *Alnus nepalensis*. It is anticipated that this study will be a valuable tool for forest managers, forest users and researchers and to contribute to the carbon trade programs of Nepal within the international community.

## MATERIALS AND METHODS

### *Study Site*

We carried out this study in Bhakarjung Community Forest of Dhikurpokhari village development committee (VDC) of Kaski district (Figure. 1) (280 06' N to 280 36' N latitude and 83040' E to 840 12' E longitude) western Nepal. The total forest area in the district is 93649.85 ha. (46.43%) out of which 65073.61 ha. (69.49%) area is covered by Annapurna Conservation Area (ACA) and the remaining 28575.48 ha. (30.51%) is managed by District Forest Office (DFO), Kaski. The altitudinal range of this district varies from 490 meters to 8091 meters from the sea level. Its average maximum temperature is 330 C and average minimum temperature is 5.60 C and the mean annual precipitation is 3068 mm to 3353.3 mm. The forest has been managed as community forest. The forest is natural uneven and mixed in composition of *Schima wallichii* (Chilaune), *Castanopsis indica* (Dhale Katus), *Alnus nepalensis* (Utis), *Quercus semicarpifolia* (Khasru), *Rhododendron* species (Laliguras), *Bombax ceiba* (Simal) and others.

### *Sampling and Measurements*

The size variation of *Alnus nepalensis* in the study area was determined from forest management plan (operational plan). We selected individual juveniles subjectively in such a way that the selected juvenile would have adequately represented whole forest population, to represent wide variations of site quality, stand origin (natural or plantation), stand density, stand age, size and treatment (e.g. Adinugroho & Sidiyasa, 2006; Dorado et al., 2006; Edwards Jr et al., 2006). This study followed the definition of juvenile as a plant having  $\geq 30$  cm in height and

<10 cm in stem circumference at 10 cm above the ground surface (Chaturvedi et al., 2012), and measurements were made accordingly. We recorded measurement from 39 *Alnus nepalensis* juveniles. We avoided measurement from deformed, top broken, suppressed, leaning and wolf individuals. The diameter of each individual plant was measured with a vernier caliper at 10 cm above the ground level by following the rules of Chaturvedi and Khanna (2011). The selected individuals were felled from the base with a hand saw, and length (from base to top) of each juvenile was measured with a linear tape. The precisions of measurement for length and diameter of individuals are 1 cm and 1 mm, respectively. Then leaves and branches from each of the felled individuals were separated. Each component (stem, leaves, and branch) was weighed *in situ* immediately after felling and recorded at a precision of 0.1 g. Samples of the stem, leaf and branch were prepared, and carried to the laboratory for drying. Drying was carried out in an oven at 105°C until a constant weight was achieved. The weight of the samples was first recorded after 24 hours and then repeated at the interval of 8 hours. The dry weight of each component (stem, leaf and branch) of the individual juvenile was determined using the dry to fresh weight ratio estimated from the samples. The volume of stem was estimated with using xylometric method (Chaturvedi & Khanna, 2011). Then wood density of stem was determined by using following formula (Chave et al., 2006):

$$\text{Wood density}(\rho) = \frac{\text{Oven dry weight of sample}}{\text{Fresh volume of sample}}$$

A summary of the modeling data is presented in Table 1.

### **Modeling approach**

Biomass of the whole plant or its parts can be modeled as a function of diameter alone (e.g. Ajit et al., 2011; Kuyah et al., 2012; Sharma, 2011; Singh et al., 2011) or diameter or height combined together (e.g. Chapagain et al., 2014; Subedi & Sharma, 2012; Hosoda & Iehara, 2010; Rizvi et al., 2008; Ketterings et al., 2001; Senelwa & Sims, 1997), or in combination of diameter, height and wood density (e.g. Chapagain et al., 2014; Alvarez et al., 2012; Chaturvedi et al., 2012; Basuki et al., 2009; Chave et al., 2005). In this study we used all three variables singly or in combination to describe the above ground juvenile biomass of *Alnus nepalensis*. These variables are diameter alone (D, D<sup>2</sup>) and diameter and height combined (DH, D<sup>2</sup>H), wood density and diameter combined (ρD, ρD<sup>2</sup>) and wood density, diameter and height combined (ρDH, ρD<sup>2</sup>H). We developed bark biomass models by using each of the eight explanatory variables alternative, and designated first model category for a model with D alone, second model category for a model with D<sup>2</sup> and third model category for a model with DH and so on resulting in eight different model categories in total. We, hereafter, have termed them as first model category, second model category, and so on, and thus each model category contains 17 alternative models (i.e. 8 × 17 = 136 alternative models, see Table: 2 for details).

We used least square technique, which is commonly used to develop biomass models for individual trees or their parts. Among several mathematical models tested, only converged models (with significant parameter estimates) for each of the explanatory variable alternatives are considered for analysis. The models were estimated using “*library(minpack.lm)*” package in which *lm* (for linear models), *nls* and *nlsLM* (for non linear models) commands in R (R Core Team, 2012). The estimated models were evaluated using various criteria such as (1) significance of parameter estimates, (2) root mean squared error (RMSE), which is also known as a measure of model’s precision, (3) adjusted coefficient of determination ( $R^2_{adj}$ ) (Montgomery et al., 2001), (4) Akaike information criterion (AIC), and this is known as one of the most reliable statistical criteria to compare the estimated models (Akaike, 1972; Burnham & Anderson, 2002), (6) Graphs of residuals, scaled and quantile-quantile (q-q) plot of estimated models were also examined to check whether models had theoretical basis and biological logics (Alder, 1995; Zeide, 1993; Goelz & Burk, 1992). Unless otherwise specified, we used 0.05 ( $\alpha = 5\%$ ) level of significance in our analyses.

## RESULTS AND DISCUSSION

Parameter estimates of 108 models out of 136 models ( $8 \times 17 = 136$  models or 18 models in each model category, see Table 2 for details) were significant. This shows that most of the models (108 significant models) tested in this study are appropriate to the data. There was still a significant portion of residuals variation left unexplained (RMSE = 42 g) though our models showed promising fits to the given data. It is obvious that any of the mathematical models cannot perfectly describe the data of all survey everywhere (Hasenauer & Monserud, 1997; Montgomery et al., 2001; Ratkowsky, 1990). Therefore, the biometricians need to test several candidate models of various mathematical forms (linear, power, parabolic, exponential, and asymptotic) to their data which could offer good chance to get more suitable model to the data (e.g. Ajit et al., 2011; Fang & Bailey, 1998; Huang et al., 1992; Ratkowsky, 1990; Rizvi et al., 2008; Sharma et al., 2011). Among 136 alternative models, fit statistics and parameter estimates of only best model in each model category are listed in Table 3. M9 from fourth model category, M6 from eighth model category and M2 from first model category showed the best fits (smallest RMSE, AIC and largest  $R^2_{adj}$ ) among the models. The first model M1, the most versatile equation to develop biomass model (Sharma, 2011; Miksys et al., 2007; Ter-Mikaelian & Korzukhin, 1997), appeared in the tenth, sixth, fourth, fourth, ninth, first, first and second rank within the models from the first, second, third, fourth, fifth, sixth, seventh and eighth model category, respectively. From the evaluation of fit statistics, M9 seems to be the most accurate and precise among the fourth model category and followed by the models M6 of the eighth model category, M2 of first model category, M15 of second model category, M6 of fifth model category, M14 of third model category, M1 of seventh model category and M1 of sixth model category. Graphs of model residuals, scaled and normal Q-Q were also examined.

The unstandardized residuals against the fitted values with a smooth superimposed curve for model M9 from model category fourth, model M6 from model

category eighth and model M2 from model category first is shown in fig 2. Here we are looking for evidence of curvature and outliers. The graph of M9 from category fourth shows negligible curvature and outliers in comparison to remaining two models. Absence of curvature in M9 category fourth suggests us the absence of local bias in the model.

The fig 3 shows the square root of the standardized residuals against fitted value along with smooth line. Departure from horizontal lines signify heteroskedasticity, contradicting the model assumption “ $\epsilon_i$  have constant variance”, (Robinson and Hamann, 2011) but the model M9 from category fourth shows the less heteroskedasticity than other models. Similarly, fig 4 shows a q-q plot of the standardized residuals against the normal distribution. Here the ideal plot is a straight line, although modest departures from straightness are often acceptable (due to large-sample theory). Departures from a straight line in this plot may indicate non-normality of the residuals or non-constant variance, or both (Robinson and Hamann, 2011). But in our analysis, we found all the points are in a reasonably straight line which indicates the normal distribution of residuals.

Overall performance of two independent variables D and H in the form of the  $D^2H$  seems to be much promising in case of model M9 from model category fourth because it showed best fits and comparatively smaller residual deviations and better biological logics. We selected M9 from fourth model category for the prediction of juvenile biomass of *Alnus nepalensis*. The prediction of juvenile biomass for individual *Alnus nepalensis* should be made with following equation:

$$\hat{W}_i = 57.75 + 12.07(D_i^2H_i)$$

Most of the allometric equations used in this study (Table 2) have also been used to develop several biomass models in natural resource management studies. The linear models we used in this study better described the data than their non-linear counterparts, because our data cover a wide range of *Alnus nepalensis* plant sizes (Table 1). As the data which we used to develop biomass models were not sufficiently described by most commonly used explanatory variable diameter alone like in other studies (eg. Chapagain et al., 2014; Subedi & Sharma, 2012; Ketterings et al., 2001; Senelwa & Sims, 1997), inclusion of other variable (height) as additional explanatory variable improved the model fits significantly. Any of three best models (Table 3) can be applied for prediction of juvenile biomass of each *Alnus nepalensis* with a reasonable accuracy. But these models should not be applied beyond the observed data ranges (Table 1) and stand conditions different from the basis of this study.

For model application, the first best model needs diameter at above 10 cm from ground and total height, while the second best model (density dependent model) requires density, diameter at above 10 cm from ground and total height. Thus, the density dependent model requires an extra variable (i.e. species-specific wood density) whose access is difficult and costly. But the third best model requires diameter at above 10 cm from ground only. Though the model based on diameter alone is easy to use, its accuracy and reliability is less than those requiring density, diameter and height. In practice also biomass models based on diameter and height are commonly developed (e.g. Chapagain et al., 2014; Subedi

& Sharma, 2012; Hosoda & Iehara, 2010; Rizvi et al., 2008; Wang, 2006; Ketterings et al., 2001; Senelwa & Sims, 1997; Vanclay, 1994).

Model that depends on fewer and easily accessible independent variables is usually favored, and the inclusion of additional variables into the model results in over-parameterization and biased estimation (Montgomery et al., 2001; Vanclay, 1994). The biomass models which depends on density (e.g. Alvarez et al., 2012; Chaturvedi & Raghubanshi, 2013; Chaturvedi et al., 2012; Lindner and Sattler, 2012; Basuki et al., 2009; Navar, 2009a; Chave et al., 2005; Nelson et al., 1999) are expected to better describe that varies with site qualities, ages, species, stand structure, species composition, origin and so on. Density dependent models and the models depending on diameter and height are definitely more accurate and precise and have wider scope than the models with diameter alone as the former models would be more generalized ones. In practice, the height measurement is comparatively difficult, costlier and less accurate than diameter, and therefore the model based on diameter only is most preferred. In spite of its poor performance, a model M2 (third best model) depending on D only can also be used when other explanatory variables (density and total height) are not available.

A number of sampled juveniles used in this study is fairly sufficient as they adequately represent all possible site qualities, size class, and stand conditions for plant population of *Alnus nepalensis* in the study site. Size of sample used in this study is also larger than that used in other biomass studies (Chaturvedi et al., 2012; Sharma, 2011; Basuki et al., 2009). Similar to other various biomass estimation and modeling research studies (e.g. Chapagain et al., 2014; Chaturvedi et al., 2012; Subedi & Sharma, 2012; Sharma, 2011; Lambert et al., 2005), we also used destructive sampling that requires much time and financial resources, and therefore, rarely applied for large scale sample size and large geographical area. Biomass modelling from relatively small number of sampled individuals would be sufficient when they were properly representative to all possible sizes, sites and stand conditions (e.g. Chapagain et al., 2014; Subedi & Sharma, 2012; Sharma, 2011; Zianis et al., 2005; Bartelink, 1996). We could not validate the models due to lack of independent data, but further evaluations will made when the independent data are available in the future.

## CONCLUSION

Among 136 candidate models tested, a model (M9) with diameter and total height as independent variables in the form of D2H best described our data (smallest RMSE and AIC, and largest R2adj). This model explained >97% juvenile biomass of *Alnus nepalensis* with RMSE=42.34g and AIC=406.8. This model is, therefore, recommended for prediction of juvenile biomass of *Alnus nepalensis*. Application of this model is recommended to restrict to the site, size and stand condition similar to the basis of this study because this model is explicitly site-specific. Further research studies for validation, verification and re-calibration of our models with new data from wider range of site, size and stand conditions of *Alnus nepalensis* are recommended.

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**APPENDIX I: TABLES**

**Table 1: Summary statistics of data**

Diameter class	Variables	Mean±std. (range)
1-2	Diameter (cm)	1.37±0.28(1-1.98)
	Height (m)	2.06±0.61(1.15-3.2)
	Wood density (gcm-3)	0.29±0.02(0.24-0.33)
	Biomass (g)	108.23±46.27(31-227.77)
	Number	18
2-3	Diameter (cm)	2.41±0.31(2-2.96)
	Height (m)	3.49±0.69(2.8-5.05)
	Wood density (gcm-3)	0.30±0.03(0.26-0.37)
	Biomass (g)	306.38±102.93(168.1-472.46)
	Number	12
3-4	Diameter (cm)	3.27±0.22(3.05-3.17)
	Height (m)	4.69±0.82(3.55-5.9)
	Wood density (gcm-3)	0.33±0.05(0.27-0.44)
	Biomass (g)	691.97±164.85(490.2-942.89)
	Number	9
Overall	Diameter (cm)	2.13±0.82(1-3.17)
	Height (m)	3.11±1.26(1.15-5.9)
	Wood density (gcm-3)	0.3±0.03(0.24-0.44)
	Biomass (g)	303.91±252.07(31-942.89)
	Number	39

Table 2: Candidate models considered

Specification	Model form	References
M1	$Y_i = \beta_0 X_i \beta_1 + \epsilon_i$	Huxley and Teissier (1936)
M2	$Y_i = \beta_0 \exp(\beta_1 X_i) + \epsilon_i$	Rizvi et al. (2008)
M3	$Y_i = \beta_0 \exp(-\beta_1 / X_i) + \epsilon_i$	Schumacher (1939)
M4	$Y_i = \beta_0 [1 - \exp(-\beta_1 X_i)]^3 + \epsilon_i$	Bertalanffy (1949)
M5	$Y_i = \beta_0 \exp(\beta_1 / X_i) + \epsilon_i$	Modified after Schumacher (1939)
M6	$Y_i = \beta_0 + \beta_1 X_i + \beta_2 X_i^2 + \epsilon_i$	Brown (1997)
M7	$Y_i = \beta_0 + \beta_1 X_i^2 + \epsilon_i$	Sharma (2011)
M8	$Y_i = \beta_0 + \beta_1 / X_i + \beta_2 X_i^2 \epsilon_i$	Sharma (2011)
M9	$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i$	Spurr (1952)
M10	$Y_i = \beta_0 + X_i \beta_1 + \epsilon_i$	Subedi and Sharma (2012)
M11	$Y_i = X_i / (\beta_0 + \beta_1 X_i) + \epsilon_i$	Hosoda and Iehara (2010)
M12	$Y_i = X_i^2 / (\beta_0 + \beta_1 X_i) + \epsilon_i$	Modified after Hosoda and Iehara (2010)
M13	$Y_i = X_i^2 / (\beta_0 + \beta_1 X_i^2) + \epsilon_i$	Modified after Hosoda and Iehara (2010)
M14	$Y_i = \beta_0 + \beta_1 X_i + \beta_2 / X_i + \epsilon_i$	Chapagain et al. (2013)
M15	$Y_i = \beta_0 + \beta_1 X_i \beta_2 + \epsilon_i$	Sharma (2011)
M16	$Y_i = \beta_0 + X_i (\beta_1 + \beta_2 / X_i) + \epsilon_i$	Chapagain et al. (2013)
M17	$Y_i = \beta_0 X_i (\beta_1 + \beta_2 X_i) + \epsilon_i$	Sharma (2006)

Note:  $y_i$  = biomass of individual  $i$  (g),  $x_i$  = explanatory variable for juvenile  $i$  [eight explanatory variable alternatives such as (1)  $D$ ; (2)  $D^2$ ; (3)  $DH$ ; (4)  $D^2H$ ; (5)  $\rho D$ ; (6)  $\rho D^2$ ; (7)  $\rho DH$ ; and (8)  $\rho D^2H$  were considered, and eight model categories were defined accordingly];  $D_i$  = diameter of juvenile  $i$  at above 10 cm from ground (cm);  $H_i$  = height of juvenile  $i$  (m);  $\rho$  = wood density of juvenile  $i$  (gcm<sup>-3</sup>), and  $b_1, b_2, b_3$  = parameters to be estimated, and  $\epsilon_i$  = unexplained error, which was assumed to be independent and normally distributed with zero mean and constant variance.

Table 3: Fit statistics and parameter estimates of the best model of each model category (see definition of model category in Table 2)

Model category	Model	Explanatory variable*	Parameter estimates			R2 adj.	RMSE	AIC	
			$\beta_0$	$\beta_1$	$\beta_2$				
1	III	M2	D	30.20	0.94		0.9594	51.45	421.99
2	IV	M15	D2	61.32	14.89	1.56	0.9604	51.52	423.04
3	VI	M14	DH	-135.70	50.67	234.68	0.9561	54.25	427.06
4	I	M9	D2H	57.75	12.07		0.9725	42.34	406.8
5	V	M6	$\rho D$	294.35	-1055.70	429.86	0.9566	53.91	426.57
6	VIII	M1	$\rho D^2$	182.98	1.00		0.9206	71.96	418.16
7	VII	M1	$\rho DH$	130.89	0.97		0.9375	63.82	438.80
8	II	M6	$\rho D^2H$	12.16	45.06	-0.46	0.9642	48.94	419.02

\* $D$  = diameter at 10 cm from ground (cm);  $H$  = total height of juvenile (m);  $\rho$  = wood density of juvenile (gcm<sup>-3</sup>); all other symbols are the same as defined in Table 2, Eq. 2, and section of modelling approach.

APPENDIX IV: FIGURES

Figure 1: Location of study site

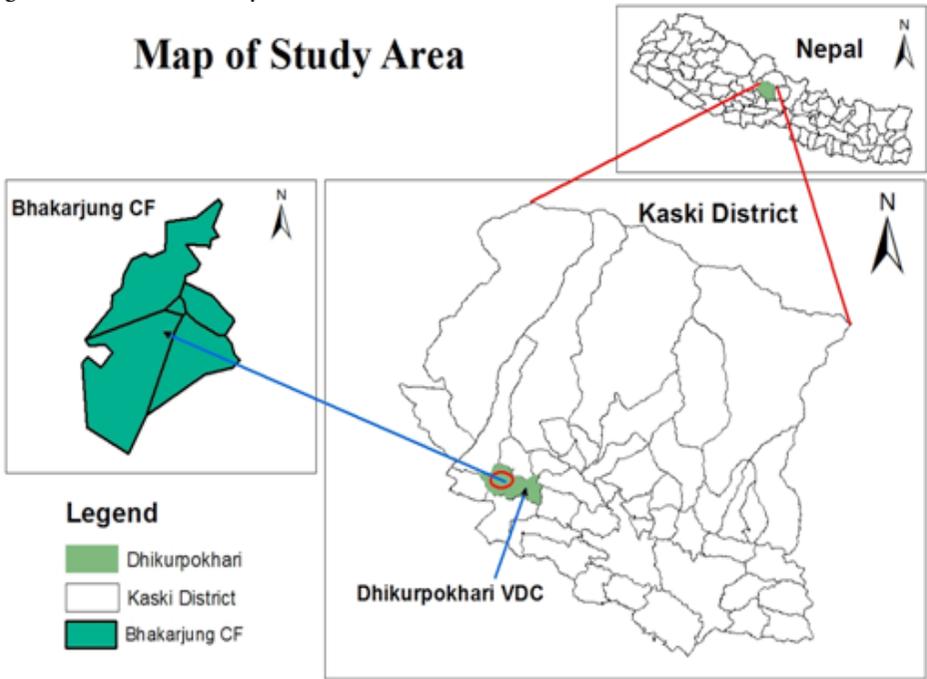


Figure 2: Residual vs Fitted value

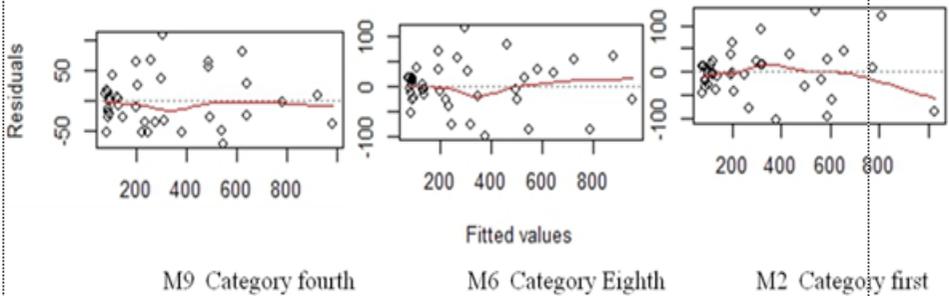


Figure 3: Scale location

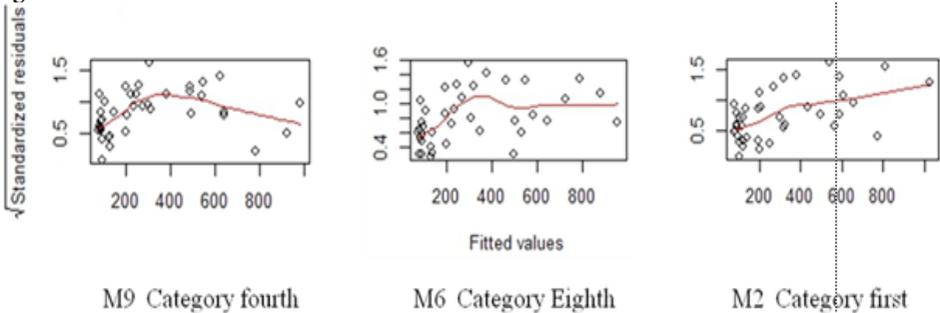
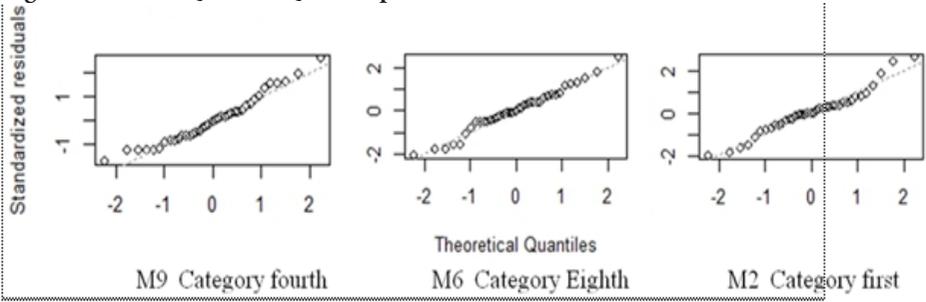


Figure 4. Normal Quantile-Quantile plot



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