A remote sensing-based approach for water accounting in the East Rapti River Basin, Nepal

Rajendra L Shilpakar1,*, Wim GM Bastiaanssen2,3 and David J Molden4,5

1 Riverine Landscape Research Lab, Geography and Planning, University of New England, Armidale, NSW 2351, AUSTRALIA
2 Delft University of Technology, Stevinweg 1, 2600GA Delft, The NETHERLANDS
3 eLEAF and Water Watch Foundation, Generaal Foulkesweg 28, 6703 BS Wageningen, The NETHERLANDS
4 International Centre for Integrated Mountain Development, Kathmandu, NEPAL
5 Formerly, International Water Management Institute, Colombo, SRI LANKA
* For correspondence, e-mail: rshilpak@myune.edu.au

Accurate estimates of evapotranspiration across different land uses are a major challenge in the process of understanding water availability and uses in a river basin. This study demonstrated a remote sensing-based procedure for accurately generating evapotranspiration and runoff in mountainous areas using Landsat ETM+ images combined with standard hydro-meteorological data. The data was used as a key input into the International Water Management Institute (IWMI)’s water accounting procedure to understand how water is now used, and opportunities for improvements in the future. We found a higher annual actual evapotranspiration from the riparian forest than from irrigated agriculture in the East Rapti River basin of Nepal. Another important finding of our study is that simple rainfall surplus can be a good predictor of river flow at an ungauged site of the East Rapti River basin. The water accounting analysis revealed that there is the potential for further development of water resources in the East Rapti River basin as only 59% of the total available water is depleted. A critical analysis of social and ecological flow requirements downstream is necessary before any development of water resources upstream. This study successfully demonstrated that the key inputs required for evaluating and monitoring the overall water resources conditions in a mountainous river basin can be computed from satellite data with a minimal support from ground information.

Key words: water accounting, remote sensing, SEBAL, evapotranspiration, rainfall surplus, evaporative depletion, East Rapti River basin

Water scarcity in many large river basins of Asia will increase significantly due to rapid urbanization, industrialization, increased need for food and agricultural demands, economic development (CA 2007), and climate change (IPCC 2007). This increase in water demands for human uses, combined with the need to retain sufficient water for environmental uses has placed many river basins under stress (Smakhtin et al. 2004). Increased withdrawal of water for agriculture to meet increasing demands for food will alter river flow patterns and affect other uses such as environmental uses in the ways that are not immediately obvious. Hence, efforts to improve water management require better understanding of current water availability and uses in order to overcome problems of scarcity and competition on a longer time scale.

Researchers have pointed out that new methodologies and terms are needed to describe clearly the actual use and physical losses of utilizable water from a hydrologic system (Willardson et al. 1994, Allen et al. 1997). Water accounting is a tool employed to help users in a hydrological domain to understand their resources. The International Water Management Institute (IWMI) developed a water accounting procedure to classify water balance components into water use categories that reflect the consequences of human intervention in the hydrologic cycle (Molden 1997, Molden and Sathakhavdiev 1999, Cai et al. 2002). IWMI’s water accounting framework focuses on supply and total depletion of water as opposed to only withdrawals. Thus, the water accounting framework relies on estimates of actual evapotranspiration, as evaporative depletion (consumption) is a main component of total water depletion in a river basin. Actual evapotranspiration reflects the real conditions in the fields, as opposed to the reference evapotranspiration that pertains to a hypothetical land surface (Allen et al. 1998). An updated version of IWMI’s water accounting framework (WA+) is under development (Karimi et al. 2012). WA+ is based on 4 sheets that describe the water resources, water depletion, land and water productivity, and water withdrawals. In this framework, land use and land cover classes and their benefits for agriculture, economy and environment are explicitly described (Karimi et al. 2012). WA+, a remote sensing data based water accounting framework, can be applied when ground data are not available or not accessible.

Accurate estimation of actual evapotranspiration (ETa) is a key challenge for analyzing water availability and water consumption in a river basin (Perry 2007). ETa is typically estimated based on climatic parameters recorded...
in representative weather stations and extrapolated for the larger area or computed as a residual term in water balance equations. Such approaches lead to significant overestimation of \( ET_a \) in water shortage conditions because soil moisture and leaf area development are in reality binding constraints (Bastiaansen et al. 2007). Remote sensing technologies and techniques show promise for improving estimates of \( ET_a \) at different spatial scales and in separate scenes, based on land use (e.g. Allen et al. 2011, Bastiaansen and Bandara 2001, Kustas et al. 2003). For example, Jackson et al. (1977) performed pioneering work on thermal infrared applications for assessing \( ET_a \) fluxes, which was followed by development of several new \( ET_a \) algorithms using remotely sensed measurements (see reviews by Kustas et al. 2003, Coutroud et al. 2005, Kalma et al. 2008, Allen et al. 2011). Many of these methods were developed and validated in a flat landscape. Applying them to regions with rough topography where ground truth points are lacking (e.g. Himalayan region) has proved difficult.

Nepal is known to have great water resources potential. The renewable surface water available in the country is estimated to be about 22.5 billion m³ per annum (UN 2000). Surface water availability is more than 9,000 m³ per capita per annum, which is many times more than the ‘water stress index’ of 1,700 m³ per capita per annum (Falkenmark et al. 1989, Tourre et al. 2012). But the magnitude of annual surface water availability as presented here may be misleading, as there is high spatial and temporal variability in water availability in Nepal due to the contrast between the swollen rivers typical of summer monsoon and the desiccated land during the dry season. Many people in Nepal remain water insecure, because access to water remains difficult throughout the year for household and agricultural use. To guide decisions regarding the use of water, the relationship between its availability from renewable resources and its consumption must be quantitatively described. The relationship is not straightforward due to the heterogeneity and complexity of hydrological processes combined with a scarcity of data in most of the river basins and catchments in the country.

This study aims to demonstrate how satellite remote sensing images can be effective in providing the key information on the hydrological behavior of a river basin at various spatial scales, ranging from local catchments to the entire river basin. We focus on the quantification of (i) river flow in ungauged watersheds, and (ii) evaporative depletion by agriculture and the environment (natural vegetation) in a Himalayan river basin.

Materials and methods

Basin setting

The East Rapti River basin, comprising an area of rapid urban and agricultural development and also an important nature conservation area (Chitwan National Park), was selected for demonstrating remote sensing and GIS approach for elucidating \( ET_a \) existence and availability and uses at two scales — entire river basin and the relatively small catchments within the basin. The East Rapti River basin extends from 27°21’23”N to 27°47’00”N latitude and 84°08’43” to 85°11’57”E longitude, covering a total area of 3,084 km². The East Rapti River originates from a catchment in the Mahabharat mountain range about 25 km southwest of Kathmandu, and merges with the Narayani River, an international river that drains towards India, where it is known as the Gandak (Figure 1). The north- eastern part of the basin is mountainous with a maximum elevation more than 2,600 m asl, while the elevation of downstream areas in the western part of the basin normally does not exceed 300 m asl. The East Rapti River joins the Narayani River at an elevation of 140 m asl.

The climate of the basin is humid and subtropical. The average annual rainfall is 2,008 mm, as estimated from the rainfall data recorded at the seven rainfall stations (see Figure 1) within the basin from 1976–2001. More than 80% of the total annual rainfall occurs during the four month monsoon season from June to September, July and August are the wettest months, receiving nearly half of the annual rainfall. The average temperature at Rampur station (181 m asl) during the hottest month, June, is about 30°C. The average daily temperature for the same month at Daman (2,380 m asl) is only about 18°C. January is the coldest month in the basin with an average daily temperature of 15°C at Rampur and about 7°C at Daman.

More than 80% of the economically active populations are involved in agriculture. However, about 46% of agricultural households own less than 0.5 ha of land indicating the subsistence nature of agriculture (Ghimire et al. 2000). Rainfed agriculture is practiced in mountainous areas of the basin. In the valleys, water from seasonal streams and tributaries is tapped for domestic, irrigation and livestock purposes. In the middle reaches of the basin, known as East Chitwan, more than 94 small irrigation systems exist, providing supplementary irrigation to about 9,500 ha of agricultural land. In the most downstream part of the basin (West Chitwan), irrigation water is drawn from the Khageri Khola (a tributary of East Rapti River) and the Narayani River (Smakhtin and Shilpakar 2005). The East Rapti River basin lies in row 41 of two adjoining Landsat paths, 141 and 142. Path 141 covers about 65% of the upper part of the East Rapti basin. Because of limited budget available for satellite data purchase, we excluded some downstream portion of the basin for the analysis. In our analysis, we treated the confluence of the East Rapti and Khageri, located about 34.5 km upstream from the actual outlet of the entire basin, as the outlet of a hydrological domain that loosely represents the entire basin. For the purposes of basin scale water accounting analysis, the hydrological boundary of the outlet covering an area of 2,217 km² was treated as the water-balance domain of the East Rapti sub-basin (or simply “sub-basin” hereafter). Catchment scale analysis was carried out for the three catchments the Rajaiya, Manahari and Lothar (see Figure 1).

GIS and remote sensing data

The primary data used in this study include Landsat 7 Enhanced Thematic Mapper Plus (ETM+) images, a digital elevation model (DEM), and river flow data recorded at seven rainfall stations and three river gauges distributed within and around the basin (Figure 1, Table 1). Landsat images record information from the visible, near infrared and the thermal infrared region of the electromagnetic spectrum. The information from thermal infrared region is an essential component in estimating energy balance. Three Landsat ETM+ images for path/row 141/41 with <1% cloud cover were acquired for this study. The cloud contaminated pixels were masked out using a cloud map, which is prepared by analyzing histograms of the visible and thermal bands. The acquisition dates of images, chosen to avoid cloud contamination, were 24 October 2001, 27 December 2001 and 1 March 2002. The long-term rainfall (1976–2001) and river flow data (1963–2001) were acquired from the Department of Hydrology and Meteorology in Nepal. In addition, the hours of sunlight and mean wind speed data were obtained from the Global Water and Climate Atlas (IWMI 2000).

Estimation of actual evapotranspiration (ET \(_a\))

Surface Energy Balance Algorithm for Land (SEBAL) is an algorithm that uses satellite-derived surface albedo, surface temperature and vegetation index, along with routine weather data such as wind speed and humidity, to compute spatial variation in net radiation (\( R_n \)), soil heat flux (\( G \)) and sensible heat flux (\( h \)) on a pixel-by-pixel basis (Bastiaansen et al. 1998, 2002, 2005, Teixeira et al. 2009). The latent heat flux \( (\lambda E) \) is computed as a residual in the surface energy balance equation (Bastiaansen 2005, Boegh et al. 2002, Senay et al. 2007).

\[
\lambda E = R_n - H - G 
\]

(1)

The symbols related to Eq. (1) are explained in the text above. \( \lambda E \) is used to estimate the evaporative fraction (\( A \)).

\[
A = \frac{\lambda E}{R_n - G} \quad [-] 
\]

(2)

The ultimate goal of the whole SEBAL process is to compute daily evapotranspiration. The instantaneous evaporative fraction (\( A \)) is considered similar to its 24-hour counterpart (Shuttleworth et al. 1989, Brutsaert and Sugita 1992). Hence, the SEBAL-driven instantaneous evaporative fractions can be used to compute actual 24-hour evaporation using Equation 3 (Bastiaansen et al. 2000).

\[
ET_{24} = A \cdot ET_a 
\]

(3)

where \( ET_a \) is the 24 hours actual evapotranspiration, \( R_n \) is the 24 hours net radiation, and \( \lambda E \) is computed as a residual in the surface energy balance equation (Bastiaansen 2005, Boegh et al. 2002, Senay et al. 2007).
The components of SEBAL are described in detail in Bastaaianssen et al. (1998). A list of equations and symbols involved in SEBAL procedure is provided as Appendix 1; an elaborated list of procedures followed in this study is available in Shlipak (2003): Only the specific terrain related components of the SEBAL will be discussed in this paper (Allen and Tasumi 2008, Tasumi et al. 2008, Morse et al. 2001). The terrain-corrected components include solar radiation for computing net radiation at the land surface \( R_s \), surface-to-air temperature differences for estimating the sensible heat flux \( H \), and the psychrometric constant and air density for computing sensible heat flux \( H \) and latent heat flux \( LE \).

The solar incident angle is one of the key components of the net radiation at the land surface \( R_s \). In the mountainous landscape, the value of solar incident angle \( \theta \) is highly dependent on surface slope and aspect. Hence, Equation 4 needs to be applied for computing cosine of \( \theta \) for non-flat surface. It computes the solar incident angle for each pixel separately (at 30m x 30m pixel resolution to match with Landsat data) and incorporates the effect of slope and aspect for an instantaneous time scale (see Duffie and Beckman 1991, Allen et al. 2007):

\[
\cos \theta = \sin \phi \sin \lambda \sin \delta \sin \alpha \cos \phi \sin \alpha + \cos \phi \cos \alpha \cos \delta \cos \phi \sin \alpha + \cos \phi \sin \alpha \sin \delta \sin \phi \sin \alpha \sin \delta \sin \phi \sin \alpha
\]  
\( \text{(4)} \)

where \( \delta \) is the declination of the earth (positive in summer in northern hemisphere), \( \phi \) is the latitude of the pixel in radians (positive for northern hemisphere), \( \alpha \) is the slope in radians, where \( \alpha = 0 \) is horizontal and \( \alpha = \pi / 2 \) is vertical downward (\( \alpha \) is always positive and represents a downward slope in any direction), \( \gamma \) is the deviation of the normal to the surface from the local meridian, where \( \gamma = 0 \) for aspect that is due south or the south facing slope, and \( \gamma = \pi / 2 \) represents a north-facing slope with \( \gamma = -\pi / 2 \) represents an east facing slope and \( \gamma = +\pi / 2 \) represents a west-facing slope), and \( \phi \) is the hour angle, where \( \phi = 0 \) at solar noon, \( \phi \) is negative in morning, and \( \phi \) is positive in afternoon.

Using the slope and aspect corrected cosine of solar incident angle, the total instantaneous extra-terrestrial solar radiation \( K'_{0e} \) for each pixel can be computed using Equation 5.

\[
K'_{0e} = G_s \cdot d_s \cdot \cos \theta \text{ [W m}^{-2}\text{]} \]  
\( \text{(5)} \)

where \( G_s \) is the solar constant \( [1.367 \text{ Wm}^{-2}] \), \( d_s \) is the inverse relative earth-sun distance in astronomical units [AU].

By integrating incoming radiation from sunrise to sunset, we can compute the total incoming extra-terrestrial solar radiation \( K'_{0e} \) for 24 hours using Equation 6.

\[
K'_{0e} = G_s \cdot d_s \cdot \int_0^{\pi / 2} \cos \theta \ d\theta \text{ [W m}^{-2}\text{]} \]  
\( \text{(6)} \)

where \( \omega_0 \) and \( \omega_f \) are start- and end-end sun hour angles indicating when the Sun’s rays first strike and disappear from the Earth’s surface.

For a horizontal surface, \( \omega_0 \) and \( \omega_f \) are equal to \( \omega_0 \) and \( \omega_f \) as the sunset hour angle. Allen and Tasumi (2000) suggest that Equation 6 can be solved for each half-hour time step during the day, and then integrated numerically. Here, the value \( \omega \) varies from \( -\pi / 2 \) to \( \pi / 2 \) by radians of 0.5/12 radian.

Estimation of \( H \) requires an estimate of the surface-to-air temperature difference \( \Delta T \). In SEBAL, \( \Delta T^d \) is estimated as a linear function of surface temperature. Surface temperature was computed from the thermal infrared band of Landsat 7 images (i.e. Band 6). For mountainous landscapes, Band 6 in Landsat needs to be adjusted to a common reference elevation for an accurate prediction of \( \Delta T \). Otherwise, high elevations that appear to be ‘cool’ will be associated with evaporative cooling. Therefore, a “lapsed” surface-temperature map was made to assist in computing surface-to-air temperature differences. A pixel in the flat area (Chitwan valley) with an elevation of 118 m was identified as a datum for computing the lapsed surface temperature as follows:

\[
T_{s,\text{lapse}} = T_s + 0.0065 \cdot \Delta z \text{ [K]} \]  
\( \text{(7)} \)

where \( T_s \) is the surface temperature in \( K \) derived from Band 6 of the Landsat image and \( \Delta z \) is difference between the pixel’s value (elevation) and the elevation of the datum in meter.

The surface-to-air temperature difference \( \Delta T \) is a key input for computing the sensible heat flux \( (H) \). Assuming, the \( \Delta T \) has a linear relation to the lapse temperature \( T_{lapse} \), the surface-to-air temperature difference map can be computed using Equation 8.

\[
\Delta T = a + b \cdot T_{lapse} \text{ [K]} \]  
\( \text{(8)} \)

where \( a \) and \( b \) is constant internal that prescribe the sensible heat flux \( (H) \) to remain in a range defined by the user.

The constants \( a \) and \( b \) can be estimated using the “internal calibration” procedure as explained by Allen et al. (2007). In the process, the lower end of \( \Delta T \) is associated with “hot pixel with maximum \( T_{lapse} \)”, where the available energy is dissipated to sensible heat flux \( (H) \). For the East Rapti River basin, a pixel associated with a well-watered and well vegetated area in the flat valley area near the river was considered as “hot pixel”. A pixel in the dry sandy areas in the river bed was identified as “hot pixel”.

Atmospheric pressure \( (P) \) is another parameter required to compute actual evapotranspiration from remote sensing data. The atmospheric pressure was computed from the elevation data (i.e. Digital Elevation Model) using Equation 9, as suggested by Allen et al. (1998) for the mountainous landscape:

\[
P = 101.3 \left(293 - 0.0065 \cdot \eta \right) / 293 \text{ [kPa]} \]  
\( \text{(9)} \)

where \( \eta \) is the elevation in meters.

The atmospheric pressure allows the computation of air density \( (\rho_a) \) and the psychrometric constant \( (\gamma) \) can then be modeled using Equation 10:

\[
\rho_a = P / (T_a \cdot R) \text{ [kg m}^{-3}\text{]} \]  
\( \text{(10)} \)

where \( R \) is the specific gas constant \([0.287 \text{ kJ kg}^{-1} \text{K}^{-1}]\), and \( T_a \) is the virtual temperature \([\text{K}]\) computed from mean air temperature.

\[
\gamma = \frac{c_p}{\lambda} \cdot \frac{P}{R} \text{ [kPa}^{-1} \text{C}^{-1}] \]  
\( \text{(11)} \)

where \( c_p \) is the air specific heat \([1 \text{ kJ kg}^{-1} \text{C}^{-1}]\), \( \lambda \) is ratio of molecular weight of water vapor/dry air \([0.622]\), \( q \) is latent heat of vaporization \( [2.45 \text{ MJ kg}^{-1} \text{H}] \), and \( \gamma \) is aerodynamic resistance \([\text{m s}^{-1}]\).

The \( r_s \) is computed for the date of satellite overpass, and it is assumed that the values are representative for the monthly average values during which that image has been acquired. While this assumption can only be verified by analyzing more Landsat images, it can be used as a first approximation of \( r_s \). A simple linear interpolation technique was used to compute monthly \( r_s \) for other months. The minimum \( r_s \) values were restricted to 80 s m\(^{-1}\) for the wet months having monthly rainfall greater than 200 mm. The outputs from equations (4) to (11) were also incorporated into the Penman-Monteith equation to get monthly \( ET_a \).

We also prepared monthly reference evapotranspiration \( ET_r \) maps for 12 months following FAO 56 (Allen et al. 1998) with net radiation corrected for slope and aspect. The ratio of \( ET_r/ET_a \) which we term the “relative coefficient,” was used to...
Box 1. Definition of water accounting components (adapted from Molden, 1997 and Molden and Sakthivadivel, 1999)

Gross inflow (GI) is the total amount of water entering into the water balance domain from precipitation and from surface and subsurface sources.

Net inflow (NI) is the gross inflow plus any changes in storage. If water is removed from the source over the water accounting time period, net inflow exceeds gross inflow; if water is added to storage, net inflow is lower than gross inflow.

Depletion (D) is consumption or removal of water from a water basin that renders it unavailable or unsuitable for further use. Water is depleted in four ways:
- evapotranspiration, i.e. water is vaporized from surfaces or transpired by plants;
- flow to sink, i.e., water flows into a sea, saline ground water, or other location where it cannot economically be recovered for further use;
- pollution, i.e. water quality is degraded to such an extent that it is not suitable for certain uses; incorporation into product, as, for example, the assimilation of irrigation water into plant tissues.

The depletion is beneficial if water is depleted in providing an input to produce a good such as an agricultural output, or any other manner deemed beneficial such as ecosystem services. Beneficial depletion can further be classified into process and non-process. Process depletion (PD) is that amount of water which is depleted to produce a human-intended product such as water diverted for crop production, and water consumed by industries. Non-process depletion (NPD) occurs when water is depleted naturally (or without human interfered process like irrigation) such as evapotranspiration by natural forests or other natural vegetation. Non-process depletion can be either beneficial or non-beneficial.

Committed outflow (CO) is that part of outflow from the water balance domain that is committed to downstream environmental requirements or downstream water rights.

Uncommitted outflow (UO) is water that is not depleted or committed and is therefore available for use within the domain, but flows out of the basin due to lack of sufficient storage or operational measures. Uncommitted outflow can be classified as utilisable or non-utilisable.

Utilisable or non-utilisable. Outflow is utilisable if it could be consumed, given improved management of existing facilities. Non-utilisable uncommitted outflow exists when the facilities are not sufficient to capture the otherwise utilisable outflow.

Available water (AW) is net inflow minus both water set aside for committed uses and non-utilisable uncommitted outflow. It represents the quantity of water available for use at the level of basin, service, or use. Available water includes process and non-process depletion plus utilisable outflows.

A closed basin is one where all available water is depleted. An open basin is one where there is some uncommitted utilisable outflow.

In a fully committed basin, there are no uncommitted outflows. All inflowing water is committed to various uses.

Indirectly assess performance of SEBAL derived ETa.

The SEBAL derived monthly ETa maps were overlaid with a land cover class map (Figure 2) in order to estimate ETa for each land cover class. The land cover map was derived from the same Landsat images (see Shilpakar 2003). A combination of supervised classification and band ratio method (Meijerink et al. 1994) was applied for the land cover classification using the field sample points collected in October 2002.

Estimation of basin rainfall and river runoff

The distance from the Indian Ocean is an explanatory parameter for the spatial variability of rainfall. An analytical relationship between distance to ocean and rainfall has been established and used as the basis for the determination of spatial distribution of rainfall across the basin. Multiple regression equations for each month were derived using long-term (1976–2001) mean monthly rainfall, elevation, latitude and longitude of the seven rainfall stations within and around the basin (Shilpakar 2003). These monthly regression equations were fitted to estimate the spatial distribution of monthly rainfall for the entire basin using the spatial position (i.e. latitude, longitude) and elevation of each pixel.

Traditionally, river runoff has been estimated from rainfall events, soil properties, antecedent moisture and vegetation cover using empirical equations (Schaake et al. 1996). Bastiaanssen and Chandrapala (2003) suggested a simple and novel method of estimating river runoff using rainfall surplus (rainfall minus evapotranspiration), assuming negligible net infiltration. A similar method was applied in this study in order to estimate river runoff at ungauged sites. The monthly rainfall surplus (Sp) for every pixel was taken as the difference between monthly rainfall (R) and ETa as follows:

\[ Sp = R - ETa \]  \[ (13) \]

The rainfall surplus will not be immediately translated into surface runoff. There is a delayed response in the catchment between rainfall and stream flow due to infiltration, recharge, storage mechanisms, and subsequent interactions between groundwater and surface water. These delays are accounted for by calculating two-month moving average of monthly rainfall surplus (Spavg).

Spavg = (Sp + Sp) / 2  \[ (14) \]

where Sp is the rainfall surplus for the previous month.

Spavg was then used to estimate river runoff depth for the sub-basin by analyzing its relationship with observed runoff depth for the Rajaiya catchment. Out of three gauging stations that measure river flow in the East Rapti River basin (Figure 1), the Rajaiya station was selected for calibrating catchment rainfall surplus, as the river runoff-depth relationship at this catchment can be considered topographically more representative of the sub-basin. The observed river flow data for the Rajaiya station were converted to runoff depth from the catchment on a monthly time scale. The relationship between Spavg and runoff depth was used to estimate the runoff depth for the sub-basin (see Shilpakar 2003).

Estimation of water accounting components

The water accounting process described by Molden (1997) and Molden and Sakthivadivel (1999) was followed in this study. The water accounting procedure quantifies total
Table 3. Monthly values of relative coefficients (ET/aET) for major land cover classes

<table>
<thead>
<tr>
<th>Land cover</th>
<th>ET (mm)</th>
<th>aET (mm)</th>
<th>Relative coefficients (ET/aET)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Forest</td>
<td>1028</td>
<td>0.83</td>
<td>0.75</td>
</tr>
<tr>
<td></td>
<td>946</td>
<td>0.62</td>
<td>0.77</td>
</tr>
<tr>
<td></td>
<td>753</td>
<td>0.33</td>
<td>0.47</td>
</tr>
<tr>
<td></td>
<td>538</td>
<td>0.34</td>
<td>0.58</td>
</tr>
<tr>
<td></td>
<td>946</td>
<td>0.55</td>
<td>0.71</td>
</tr>
<tr>
<td></td>
<td>1217</td>
<td>0.87</td>
<td>0.88</td>
</tr>
<tr>
<td></td>
<td>80</td>
<td>0.66</td>
<td>0.05</td>
</tr>
</tbody>
</table>

Results and discussion

Surface Energy Balance Algorithm for Land

The Surface Energy Balance Algorithm for Land (SEBAL) is used to compute the partitioning of net solar radiation available at the land surface to the sensible heat flux, latent heat flux and the soil heat flux. Energy partitioning can be expressed as the evaporative fraction (\(\lambda\)). The present study reveals that permanent forest converts a large portion of available energy into latent heat flux for evapotranspiration (\(\lambda > 0.95\)). The evaporative fraction for agricultural areas varies from 0.88 (maize) to 0.92 (rice).

Three daily ET\(_o\) maps, twelve monthly ET\(_o\) maps and one annual ET\(_o\) map were prepared using SEBAL. The mean daily ET\(_o\) for three Landsat overpass days was found to be 3.2, 1.8 and 3.6 mm d\(^{-1}\) on October 24 and December 27, 2001 and March 1, 2002, respectively. This result is reasonable, as the image dates fell just after the rainy season, when soil moisture was abundant and vegetation was healthy. Due to the low sun elevation on December 27, available energy was low and ET\(_o\) was therefore low as well. Another possible reason for the higher ET\(_o\) in March as compared to December is the fact that winter crops were only in the developing stage in December while in March they had already well on their way to maturity.

The annual ET\(_o\) rates estimated by this study are presented in Figure 4. The ET\(_o\) pattern reveals that mountainous catchments exhibit lower ET\(_o\) than valley floors in the basin. The highest annual ET\(_o\) occurred within the Chitwan National Park in the lower part of the basin. The Lothar and Manahari catchments consist mainly of mountainous areas, whereas the Rajaiya catchment consists of mountainous area as well as a small flat valley. The Rajaiya has slightly higher ET\(_o\) than the Lothar and Manahari. The Chitwan valley is comprised of intensively farmed areas and protected forests, which had greater annual ET\(_o\) than the upper reaches of the basin but slightly lower than that of the Chitwan National Park area.

Figure 4. Spatial patterns of annual ET\(_o\) in the East Rapti sub-basin (mm y\(^{-1}\)) during June 2001 to May 2002.

ET\(_o\), of 1.028 mm for the entire sub-basin. It is interesting to note that the highest annual ET\(_o\) was found in the foothill forests oriented towards the sunlit slopes (Figure 4). Higher solar radiation per unit area on the sunlit slope than on other slopes and abundant soil moisture in the foot hills mainly due to surface flow probably have caused the higher ET\(_o\) from the forest located in river valleys than that from surrounding agriculture areas. A maximum annual ET\(_o\) of 1.478 mm was found in forest on the sunlit slopes of valleys, where the reference evapotranspiration ET\(_{ref}\) for the forest was 1,411 mm. This gives a relative coefficient (i.e. ET\(_o\)/ET\(_{ref}\)) of 1.05, which is in good agreement with the crop coefficient reported for many fruit trees in well watered condition and forested wetlands (Allen et al. 1998). Water body had an annual ET\(_o\) (1,217 mm y\(^{-1}\)) with a relative coefficient close to one. Bushlands with mixed vegetation (short woody plants and tall grass), exhibit an annual ET\(_o\) of 1,063 mm. This slightly higher ET\(_o\) than agriculture lands may be because the bushland has an aerodynamically rough surface. However, the extent of bush area in our study area was relatively low and the contribution to the total ET\(_o\) of the basin is limited. Agricultural lands showed an average annual ET\(_o\) of 960 mm y\(^{-1}\) with ET\(_o\)/ET\(_{ref}\) of 0.76. The lowest ET\(_o\) was as low as 1 mm d\(^{-1}\) for the areas associated with unclassified land use class, the shadows in steep slope areas where there was no direct sun light. Equation 1 corrects for the effect of slope aspect in incoming radiation from the sun, but it does account for diffused atmospheric radiation. Consequently, our calculations of ET\(_o\) for those pixels may be too low.

According to a previous study (IWMI-Nepal 2000), the average annual ET\(_o\) in the East Rapti River basin was 290 mm for agricultural land, 718 mm for dense forest, and 629 mm for grassland. These figures were significantly lower than the estimates from this study. In previous study, ET\(_o\) was computed based on effective rainfall (i.e., the proportion of rainfall that reached the ground) and ET\(_o\). The ET\(_o\) was taken to be equal to ET\(_o\) if effective rainfall was equal to or greater than ET\(_o\); otherwise, ET\(_o\) was taken to be equal to effective rainfall except in the case of fully irrigated areas, where ET\(_o\) must always be equal to ET\(_o\). The main error in previous method is that it does not account for ET\(_o\) from soil moisture during the months with lower levels of effective rainfall. Only 7% of the average annual rainfall occurs during the period from October to June; consequently, evapotranspiration contributions during this period come from the root zone depth soil moisture, a factor not accounted for in previous ET\(_o\) estimates. Another potential error derives from the fact that calculations of ET\(_o\) at the reference station (located in Chitwan valley) do not take into account the large spatial variations in climatic conditions across the basin.

Using terrain-corrected ET\(_o\) and SEBAL-derived ET\(_o\), we computed the relative coefficient (ET/aET) for each land cover type (Table 3). A monthly relative coefficient close to one indicates that ET\(_o\) and ET\(_o\) are similar, which is physically possible if the soil is wet and fully covered by vegetation. The identification of wetness and vegetation cover on the basis of ET\(_o\)/ET\(_o\) was used in assessing SEBAL-derived ET\(_o\) for a longer period (Allen et al. 2011). The relative coefficients (ET/aET) were lowest in dry months, gradually increased from May till September when rainfall occurs, and then decreased again after the monsoon season. The monsoon starts in mid-May and cultivation of summer paddy starts in June. This explains the increase in the relative coefficient during the monsoon period.
A different way to validate the confidence of the ET values is by inferring the surface resistance $r_s$ and comparing it to published values of $r_s$ in the international literature (Bastiaansen and Bandara, 2001). The average values of $r_s$ for paddy and forest in East Rapti sub-basin were estimated to be 77 s m$^{-1}$ and 56 s m$^{-1}$ respectively. There is no monitoring of $r_s$ value in the East Rapti region nor could we find any value previously reported in the literature for this region; consequently, we were unable to validate the estimated $r_s$ values directly. However, our estimates for paddy and forest are consistent with values reported in other regions. For example, Harazono et al. (1998) found daytime rice resistance values ranging between 78 and 111 s m$^{-1}$ in Okayama (Japan). Kellibter et al. (1995) reported a $r_s$ value of 77 s m$^{-1}$ for tropical rain forest. Bastiaansen and Bandara (2001) found 63 s m$^{-1}$ for mountain forest and 66 s m$^{-1}$ for homesteads in the Kiriwadi Oya basin of Sri Lanka.

It is interesting to note that the annual ET, from irrigated lands is actually less than the ET, from adjacent rice forests in the river valleys (Figure 4). This indicates that ET, from riverine forests is at or near its potential, whereas ET, in the adjacent agriculture area varies based on the growth stage of crops. The agriculture lands remain non-vegetated between crops, which may also have attributed to reduced annual ET, for the agriculture areas. This may indicate that, at the annual scale, expansion of irrigated agriculture along riverine landscapes does not have a substantial impact on downstream flow in the East Rapti sub-basin. However, at a monthly or finer time scale the prevailing cropping pattern may alter flow pattern.

**River runoff**

The scatter plot (Figure 5) showed a high statistical correlation ($r^2=0.967$) between average monthly $Sp_r$ and observed runoff (outflow in mm). The combination of a negative value of the surplus rainfall and positive runoff in Figure 5 indicate that from November to April, river flow was derived primarily from groundwater discharge, i.e. base flow. The estimated runoff along with SEBAL-derived ET, and GIS-estimated sub-basin rainfall were used in estimating monthly inflow and outflow for the water accounting of the sub-basin. The “residual term” is the difference between all inflows and outflows plus depletions. We found an annual residual term of -23 mm for the East Rapti sub-basin, which came to about 1% of the gross precipitation of 2,011 mm. This indicates that our water balance calculation adequately reflects reality at the sub-basin scale. Comparison of observed and estimated long-term river runoff for the Manahari catchment reveals that estimated runoff is consistent with observed runoff during dry months, while the model underestimates peak flows (Figure 6). The underestimation of peak flow will have less influence on the overall performance indicators because a large portion of peak flow was considered non-utilizable in our water accounting assumptions (see non-utilizable outflow in Table 2). It can be concluded from this analysis that in absence of short and long term water storage options, river runoff can be estimated as a function of rainfall minus ET. This may be a breakthrough in approaching the problem of lack of flow records in ungagged basins (Thompson et al. 2011), a persistent and prevalent constraint in evaluating water resource management conditions at the scale of the river basin.

**Water accounting components**

We used the hydrological boundary of the confluents Khagari and East Rapti Rivers to define the hydrological domain of our water accounting analysis. Three catchments, Rajaiya, Manahari, and Lothar, were selected for catchment scale water accounting analysis. Table 2 illustrates water accounting components and a description of assumptions adopted for water accounting of the East Rapti sub-basin.

Water accounting analysis results for the sub-basin and the selected catchments are illustrated in Figure 7 and the computed indicators are presented in Table 4. Our water accounting analysis demonstrates that only 59% of the available water was depleted within the domain of the East Rapti sub-basin, while the remaining 41% of available water leaves the sub-basin as utilisable outflow (Figure 7a). Since utilisable outflow from the sub-basin takes place throughout the year, the East Rapti sub-basin is an ‘open basin’. On the catchment scale, a slightly smaller proportion of the available water was depleted within the domain than in the sub-basin (Figure 7b, c, and d). The East Rapti sub-basin may have a potential for further water resource development without adverse downstream effect. However, caution is required as no critical analysis of downstream environmental flow requirements currently exists for the basin despite a preliminary analysis by Smahklin and Stililpaprak (2005) and Smahklin et al. (2006).

The process fraction of available water was found to be 17% for the sub-basin, which indicates that only a small portion of available water was depleted by human intended processes (Table 4). A slightly higher value (20%) was found for Rajaiya, while both Manahari and Lothar showed smaller process fractions of available water (11%). This was due to the fact that the Rajaiya catchment included the municipality of Hetauda as well as the Hetauda Industrial Area. The beneficial utilization of available water was 57% for the sub-basin and 46%, 52% and 51% for the Rajaiya, Manahari and Lothar...
catchments, respectively. The similarity of the numbers for fractional benefit and total depleted fraction indicates a near total absence of non-beneficial depletion in the East Rapti sub-basin.

Summary and conclusions

A rational water management plan cannot be undertaken without understanding where and how much water is available and where and how much water is consumed in a given river basin. Water accounting is a procedure for classifying water balance components into water use categories; it helps planners understand water depletions and unutilized outflows. One paramount factor in water accounting analysis is data availability on actual evapotranspiration. This study shows that SEBAL, supplemented by a mountain radiation model, can be applied in assessing evaporative depletion in the mountain environment where remotely sensed satellite data are available. This study reveals that annual ETo from the perennial vegetation of the river valleys is higher than that of adjacent agriculture areas. Without remote sensing technology, this phenomenon could only be identified after intensive in situ measurements with advanced instrumentation.

Another important aspect of this water resources research study is the prediction of stream flow. A high statistical correlation (r = 0.96) between Sp_rain and river flow for the East Rapti sub-basin. Thus, rainfall surplus appears to be a simple proxy of river runoff, and this characteristic can be employed to estimate runoff at ungauged sites in East Rapti River basin, provided that storage unutilized outflows are well understood. Spatially distributed data on rainfall surplus deserves more attention in calculating stream flow estimates in ungauged watersheds, and it is an attractive alternative to (i) empirical solutions of runoff coefficients, (ii) inclusion of sophisticated distributed hydrological models, and (iii) installation of expensive hydro-meteorological stations. The combination of remotely sensed land use and water use information together with rainfall data and a digital elevation model from GIS systems gives us the capability to assess the major requirements for river accounting.

Our water accounting analysis in the East Rapti sub-basin showed that it is an open basin as there was year round outflow of utilisable flow. Only 59% of available water was depleted in the sub-basin. The remaining 41% of available water is leaving the sub-basin as utilisable outflow. This indicates that there is a potential for further development of water resources in the basin in order to increase beneficial use of the available water. However, any water resources development in the basin must be supported by a comprehensive analysis of the socio-environmental-water requirement for the riverine functions (Smakhtin et al., 2006) in the Chirwan National Park, an internationally recognized wetland site (listed as UNESCO world heritage), is located at the downstream of the East Rapti River.

Another way to increase water availability might be to exploit artificial recharge and ground water storage options in the sub-basin. Analysis of rainfall runoff indicates that a large fraction of the river flow consists of base flow (~40 mm/month). More than 90% of the annual rainfall occurs in a six-month period. In the other months, rainfall is very low and does not contribute to surface runoff. Because of the close interaction between dry weather flow and ground water storage, it is necessary to investigate and understand the interaction between river flow and ground water storage.

We have demonstrated that the remote sensing images with some routine weather and river flow data can be potentially used to compute water accounting components at different scale of a river basin such as entire basin, sub-basin and smaller catchments. Recent advances in the retrieval of radiation and moisture from satellite and digital elevation from multi-angular spectral reflectance datasets will further increase our capacity to prepare water accounts for any catchment in the world regardless of ground data coverage.

Acknowledgements

This manuscript is abstracted from the Master’s thesis of the first author. The authors are thankful to the Netherlands Fellowship Program for an MSc scholarship to the first author, and to the ITC, Wageningen, Faculty of Geo-Information Science and Earth Observations, University of Twente, the Netherlands and the International Water Management Institute (IWMI) for covering the purchase of Landsat images and other supports during the field works in Nepal in 2002. We would like to acknowledge the anonymous reviewers for their critical comments, which greatly improved this manuscript.

References


Appendix 1. A list of equations and symbols involved in SEBAL procedures

1. \( r_s = \pi L_1^2 d \cdot \frac{d}{E_{a,b}} \cdot \cos \theta \) [\( \cdot \)]
2. \( r_{a,w} = \sum_{r_s} \cdot r_{e,w} \) [\( \cdot \)]
3. \( r_{c} = \frac{r_{a,w} - r_{a,b} - r_{a,b}}{E_{a,b}} \) [\( \cdot \)]
4. \( r_{a} = 0.75 + 2 \times 10^{-3} \cdot z \cdot \) [\( \cdot \)]
5. \( \text{NDVI} = \frac{r_{a,w} - r_{a,b}}{r_{a,w} + r_{a,b}} \) [\( \cdot \)]
6. \( \text{SAVI} = \frac{(1 + L)(r_{a,b} - r_{a,b})}{L + r_{a,b} + r_{a,w}} \) [\( \cdot \)]
7. \( \varepsilon_{a} = 1.009 + 0.047 \cdot \ln(\text{NDVI}) \cdot \) [\( \cdot \)]
8. \( T_{a} = \frac{K_{a}}{L_{a} + 1} \) [\( \cdot \)]
9. \( T_{a} = \frac{T}{L} \) [\( \cdot \)]
10. \( T_{a,dom} = T_{a} + 0.0065 \cdot \Delta \zeta \) [\( \cdot \)]
11. \( L_{1} = \frac{L_{1}}{L_{1} + H + G_{s}} \) [\( \cdot \)]
12. \( R_{e} = (1 - \varepsilon_{c}) \cdot K_{d} \cdot (L_{1} - L_{1}) \) [\( \cdot \)]
13. \( K_{d} = G_{s} \cdot \cos \theta \cdot d^{2} \cdot \varepsilon_{a} \) [\( \cdot \)]
14. \( L_{1} = 1.08 \cdot \ln \left( 0.4 \cdot \varepsilon_{a} \right) \cdot T_{a} \cdot \varepsilon_{a} \) [\( \cdot \)]
15. \( q_{a} = \frac{1}{T - 273} \left( 0.0021 \cdot (\varepsilon_{a} - 0.2) \right) \cdot \ln(1 + 0.075 \cdot \varepsilon_{a}) \) [\( \cdot \)]
16. \( H = \frac{\rho_{a} \cdot C_{p} \cdot L_{1} \cdot \varepsilon_{a}}{T_{a}} \) [\( \cdot \)]
17. \( \frac{1}{L_{1}} = \frac{z}{T_{a} \cdot \varepsilon_{a}} \) [\( \cdot \)]
18. \( Z_{o} \) is under all conditions 100 m, so you can replace Zb by 100.
19. \( z_{o} = \exp(-5.809 + 5.62 \times 10^{-3} \cdot T) \) [\( \cdot \)]
20. \( r_{a} = \frac{1}{L_{1} \cdot \varepsilon_{a}} \cdot z_{o} \) [\( \cdot \)]
21. \( Z_{o} \) is under all conditions 2 m, so you can replace \( Z_{o} \) by 2 m. \( Z_{o} \) is under all conditions 0.1 m, so you can replace \( Z_{o} \) by 0.1.
22. \( \psi_{a} = 2 \ln \left( \frac{L_{1} + \varepsilon_{a}}{2} \right) + \frac{1}{L_{1} + \varepsilon_{a}} \cdot \ln \left( \frac{1 + \varepsilon_{a}}{2} \right) - 2 \cdot \text{ARCTAN}(\varepsilon_{a}) + 0.5 \pi \) [\( \cdot \)]
23. \( \psi_{a} = 2 \ln \left( \frac{L_{1} + \varepsilon_{a}}{2} \right) \) [\( \cdot \)]
24. \( x_{n} = \frac{1 - 16 \varepsilon_{a}^{2}}{L_{1}} \) [\( \cdot \)]
25. \( x_{n} = \frac{1 - 16 \varepsilon_{a}^{2}}{L_{1}} \) [\( \cdot \)]
26. \( \frac{1}{L_{1}} \cdot \frac{100}{k} \cdot \psi_{a} \) [\( \cdot \)]
27. \( \psi_{a} = \frac{L_{1}}{k} \cdot \frac{z_{o}}{z_{o} - u_{a}} \) [\( \cdot \)]
28. \( \lambda = \frac{L_{1}}{k} \cdot \frac{z_{o}}{z_{o} - u_{a}} \) [\( \cdot \)]
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H$</td>
<td>Sensible heat flux</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$G_s$</td>
<td>Soil heat flux</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$K^I$</td>
<td>Incoming shortwave radiation</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$L^I$</td>
<td>Incoming longwave radiation</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$L^O$</td>
<td>Outgoing longwave radiation</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$G_{so}$</td>
<td>Solar constant (1367 W m$^{-2}$)</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>Stefan Boltzman constant</td>
<td></td>
</tr>
<tr>
<td>$T_{ref}$</td>
<td>Surface temperature at a reference point</td>
<td>K</td>
</tr>
<tr>
<td>$c_1$</td>
<td>A factor to convert the instantaneous values of albedo to daily averages ($c_1 = 1.1$)</td>
<td></td>
</tr>
<tr>
<td>$\rho_a$</td>
<td>Air density</td>
<td></td>
</tr>
<tr>
<td>$C_p$</td>
<td>Specific heat of air at constant pressure (1004 J kg$^{-1}$ K$^{-1}$)</td>
<td>J kg$^{-1}$ K$^{-1}$</td>
</tr>
<tr>
<td>$r_a$</td>
<td>Aerodynamic resistance to heat transport</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$dT_z$</td>
<td>Vertical difference in air temperature between layers $z = z_{oh}$ and $z = z_{ref}$</td>
<td>K</td>
</tr>
<tr>
<td>$z_{oh}$</td>
<td>Surface roughness length to heat transport</td>
<td>M</td>
</tr>
<tr>
<td>$z_{ref}$</td>
<td>Reference height</td>
<td>M</td>
</tr>
<tr>
<td>$u_s$</td>
<td>Local scale friction velocity</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$u_b$</td>
<td>Average wind speed at blending height b</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$k$</td>
<td>von Karman’s constant (0.41)</td>
<td></td>
</tr>
<tr>
<td>$z_{ms}$</td>
<td>Surface roughness for momentum transport</td>
<td>M</td>
</tr>
<tr>
<td>$a$ and $b$</td>
<td>Constants</td>
<td></td>
</tr>
<tr>
<td>$L$</td>
<td>Monin-Obukhov stability length</td>
<td>M</td>
</tr>
<tr>
<td>$g$</td>
<td>Acceleration due to gravity</td>
<td>m s$^{-2}$</td>
</tr>
<tr>
<td>$\psi_a$</td>
<td>Stability correction factor for buoyancy effects on the momentum flux</td>
<td></td>
</tr>
<tr>
<td>$\psi_s$</td>
<td>Stability correction factor for heat flux</td>
<td></td>
</tr>
<tr>
<td>$\Lambda$</td>
<td>Evaporative fraction</td>
<td></td>
</tr>
<tr>
<td>$ET_a$</td>
<td>Daily (24 hours) actual evapotranspiration</td>
<td>W m$^{-2}$ [or mm d$^{-1}$]</td>
</tr>
<tr>
<td>$R_{net}$</td>
<td>Daily net radiation</td>
<td>W m$^{-2}$ d$^{-1}$</td>
</tr>
<tr>
<td>$K_{s24}$</td>
<td>Daily incoming extraterrestrial solar radiation</td>
<td>W m$^{-2}$ d$^{-1}$</td>
</tr>
<tr>
<td>$\tau_{s24}$</td>
<td>Daily atmospheric transmittance</td>
<td></td>
</tr>
</tbody>
</table>