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Amba Datt Pant

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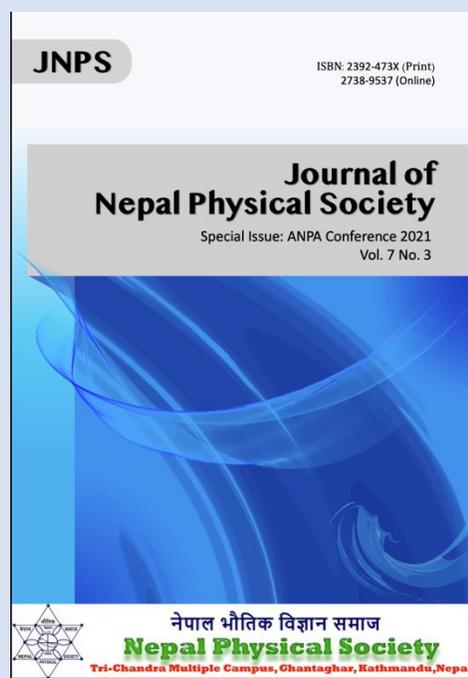
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P.O. Box: 2934
Tri-Chandra Campus
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Overview of μ SR Study in Water and Ice

Amba Datt Pant^{a)}

*Institute of Materials Structure Science, High Energy Accelerator Research Organization, 1-1 Oho, Tsukuba, Ibaraki 305-0801
Japan*

^{a)}Corresponding author: pant@post.kek.jp

Abstract. Muon spin rotation, relaxation and resonance (μ SR) method has been used to understand the properties of materials and life. In order to apply the μ SR method to life sciences, it is necessary to know the behavior of the muon and its species in different phases of water. In water, around 60% of incident muons found in the form of diamagnetic muon, around 20% in the form of muonium and remaining fraction as a missing fraction however in ice, muon and muonium are found almost 50-50% of the incident muons. The missing fraction in water is attribute to radiolysis effect. In ice, the spin dipole interaction of muon with protons will help to understand μ SR in water and in biosamples.

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INTRODUCTION

Water is an essential for functioning of life. Various life phenomena and some diseases are related to amount of water in the human body. It also plays important role for function of materials. Because of anomalous behavior of water with temperature and pressure, 17 polymorphs were reported experimentally [1]. So the behavior of water in materials varies with their phases. Even starting the study of water in materials from long ago, its various properties have not clearly understood yet.

Muon which is like a light proton acts as sensitive probe to materials in which it stops. It is available in both - positive and negative polarities in cosmic rays and accelerator facilities. Here discussion is focused on application of positive muon however the application of negative muon is out of scope of this paper. Because of fully spin polarized and asymmetric decay to positron, we can use it to understand local electronic and dynamic states of materials using muon spin rotation, relaxation and resonance (μ SR) method [2]. μ SR method has applied not only to materials sciences but also to life sciences like study of electron transfer in protein [3] and DNA [4], molecular dynamics, etc. The bound state of a muon and an electron is called as muonium ($\text{Mu} = \mu^+e^-$). The Mu is considered as a light isotope of hydrogen and shows similar chemical behavior in materials. Both charge states - muon and Mu are helpful to provide information about

the materials.

The detection of Mu in liquid was first reported by Percival et al in 1979 [5]. Then the μ SR studies in biosamples – dilute aqueous solution of DNA [6], dried horse spleen ferritin [7], ferritin and apoferritin [8], cytochrome c [3], DNA [4, 9], hemoglobin [10], enzyme [11], biosample from Alzheimer patient [12], biological aqueous solutions [13, 14] were reported. During these more than four decades, relatively slow progress of muon in life sciences with respect that in material science can be realized from the available literatures. For application of muon (using conventional and slow muon [15, 16, 17]) to life sciences, the interaction of muon and its charge states with water, and temperature and pressure dependent behavior is essentially important to separate the background signal.

In this article, an overview of μ SR study in water and ice phases is presented.

μ SR METHOD

Muon is a spin half elementary particle lies in the lepton family of second generation of the standard model of particles. The mass of a muon is about 207 times of an electron mass and 1/9 times of a proton mass. Its gyromagnetic ratio is around three times higher than that of proton ($\mu_\mu = 3.18 \mu_p$) which makes it more sensitive to materials. Two special characteristics of muon – spin po-

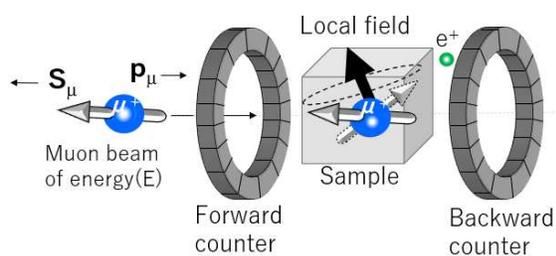


FIGURE 1. Schematic diagram of conventional μ SR experimental set up. The decayed positrons from muons are collected from the forward and backward detectors placed around the sample.

larized and asymmetric decay to positron (due to violation of parity in weak interaction) (life time $2.2 \mu\text{s}$) make the muon as an exotic tool. It works as a sensitive magnetic (spin) probe in which it stops. μ SR method provides the information about the local electronic and spin states of materials. Furthermore, it can apply without external perturbation to the system. Its time window ($10^{-11} - 10^{-5}$ s) is wider than the other techniques (NMR, neutron and Mossbauer). It stops interstitial sites near the high electron density. Its bound state with an electron known as Mu which is like a light isotope of hydrogen. It is an exotic atom made up of two lepton particles. The Mu can predict/mimic the behavior of H in the materials. For life science study, muon (μ SR) can probe the dynamics of spin, electron, proton, ions and H [2]. It also probes the dynamics of reaction, catalytic processes, concentration of molecules, magnetic behaviors, etc. and phenomena based on these processes (like electron transfer in respiratory system, photosynthesis process, diagnosis of disease, clinical and medical fields).

μ SR stands for muon spin rotation, relaxation, and resonance. The intention of the mnemonic acronym is to draw attention to the analogy with NMR and ESR. When muons are incident on material, decayed positrons are collected by detectors (forward and backward) around the sample as shown in Fig. 1. Time evolution of those positrons provide the information about the sample material. Suppose, F is positron events collected by forward counter and B is that by backward counter, then asymmetry = $(F - \alpha B) / (F + \alpha B) = A_0 G(t)$, where α is alpha factor which depends on efficiency of detectors and sample positions, A_0 is initial asymmetry, and $G(t)$ is polarization function [18]. Based on our need, we can apply external magnetic field along (longitudinal field or zero field measurement, ZF) or perpendicular (transverse field measurement, TF) to the direction of spin of the incident muon beam.

Since Mu is around 100 times more sensitive to magnetic field, Mu spectra is superposed to muon spectra. Figure 2 shows the time evolution of muon (slow rotation

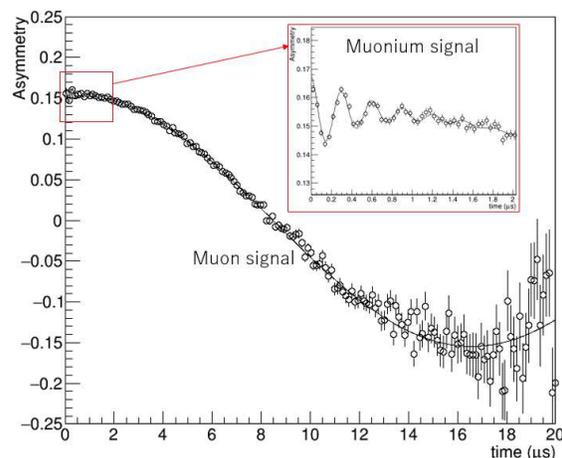


FIGURE 2. Time evolution of asymmetry in water at room temperature at transverse field 2.3 G. Muonium time spectra (inset) is superposed to muon spectra.

spectra) and Mu (fast rotational spectra) in water at TF 2.3 G at room temperature. The spectra were fitted with a function including muon and Mu sections in addition to time-independent background (Eq. 1). The fraction of muon and that of Mu formed in the sample, and corresponding relaxation rates can be extracted from the fitting of experimental μ SR data.

$$f(t) = A_{\mu} \exp(-\lambda_{\mu} t) \cos(\omega_{\mu} t + \phi_{\mu}) + A_{Mu} \exp(-\lambda_{Mu} t) \cos(\omega_{Mu} t + \phi_{Mu}) + B, \quad (1)$$

where B is the time-independent background. The terms A_{μ} and A_{Mu} are the amplitudes of the spin precession corresponding to the polarization asymmetry for the μ^{+} in diamagnetic states and Mu, respectively. The parameters λ_{μ} and λ_{Mu} are the muon and Mu relaxation rate, respectively. ω_{μ} and ω_{Mu} are the muon and Mu precession frequencies, respectively, and ϕ_{μ} and ϕ_{Mu} are the respective initial phases of their precessions. Under the transverse field of H(in G), the spins of μ^{+} and Mu take precession with the angular velocities of ω_{μ} (in kHz) = $2\pi \times 13.553 \times H$ and $\omega_{Mu} = 2\pi \times 1390 \times H$, respectively. Generally, the selection of fitting function depends on the nature of observed spectra, related phenomena, etc.

μ SR STUDY IN WATER AND ICE

When muon beam incident into water, around 60% of incident muons remained in the diamagnetic muon form and around 20% in Mu in addition to remaining missing fraction (Fig. 3). However, in ice (freezed water), there is no such missing fraction [19]. As reported by Percival et al, interaction of Mu with transient paramagnetic

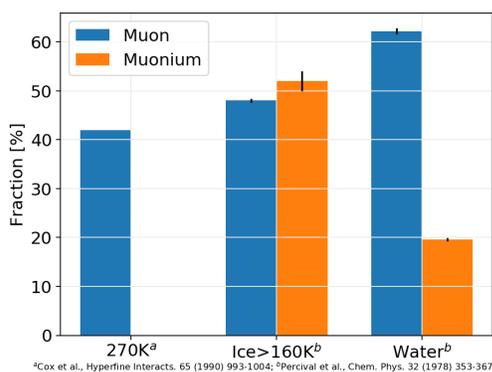
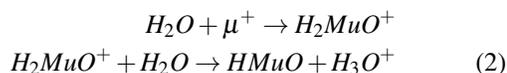


FIGURE 3. Fraction of muon and muonium in water and ice. The error bar is shown in black vertical line. The data are extracted from ref. [24] and ref. [19]

species like hydrated electron, hydroxyl radical and hydrogen atom (even small extent) formed by radiolysis of water within 100 ns is responsible for the missing fraction [20]. The intraspur reaction (muonium formation, direct generation of a fraction of the muons in diamagnetic molecules, the "missing" muon polarization) is explained based on two models - hot model and spur model [21].

Nagamine et al reported the long lived Mu in doubly distilled water [22]. However, in the presence of impurities like existence of molecular oxygen, there is relaxation of Mu due to spin exchange interaction of the Mu with paramagnetic oxygen molecules [13, 14, 23].

In addition, two steps process was reported by Percival et al and Cox et al when muon incident into water. First of all, the muon stops near the lone electron pair of oxygen and formed hydroxioum like ion (H_2MuO^+) (Eq. 2) which is similar to protonation process. Then the proton migration takes place and ultra light water (HMuO) is formed (Eq. 2).



μ SR study in ice (single crystal, hexagonal, polycrystalline) were reported by Percival et al [25, 26] and Cox et al [24, 27, 28]. The beating pattern in Mu signal obtained in ice was explained based on anisotropic diffusion of Mu in ice [29]. Llevel cross-resonance study in ice [24, 27, 28] with and without introducing defects were reported by Cox et al to understand the kinks/dips in the spectra. The stopping site and final state of muon as Mu in Bjerrum L-defect is expected however measurement in HF doped and NH_3 doped ice do not clear the image of expectation. Wang et al reported the study in various phases of ice (ice-II, ice-VI, ice-VIII and high density amorphous ice) [30] in temperature range from 5 K to 260 K. Based on the analysis of ZF μ SR data using a single exponential func-

tion, they reported the relaxation rate from ZF is higher than that from TF measurement. The initial asymmetry dropped at around 140K for ice-II, ice-VI and ice-VIII except hexagonal ice (Ih). However, the reason of distinguished behavior Ih is not clearly understood.

Mu diffuses along c-axis in the crystal even at 8 K through the quantum tunneling [31, 32]. Theoretical calculation using ring polymer molecular dynamics method by Markland et al also reported the diffusion of Mu in water and Ih ice [33]. It is mentioned that Mu diffuses from one cavity to the next along the c-axis showing agreement with experiment. Furthermore, the Mu hyperfine frequency in water at STP is reported as 4422 ± 6 MHz [34] which is smaller than that in vacuum as 4463.4 MHz [35]. Its value in ice is larger than that in vacuum value.

MUON SITE AND INTERACTION WITH H_2O

So far, the most of the previous studies focused on muonium chemistry. To my best knowledge, the stopping sites of muon in water and ice is not clearly understood yet. In pure water, if muon stops nearby the protons then the spin-dipole interaction between the muon and protons will be appeared in the experimental signal. If the muon diffuses or hops with temperature, the interaction will be changed which in turn change the nature of μ SR spectra.

Ice follows the two ice rules [36] - (1) each oxygen atom is covalently bounded by two H and (2) one H atom along the O-O vertex making covalent bond with one O and hydrogen bond with another (Fig. 4). If ice violates one of the rules, then the defect created. Incident of muon may create the defect in ice. The stopping site of muon in ice (hexagonal ice) (Fig. 4) and its spin-dipole interaction with protons will help to understand the muon behavior in ice.

For application of muon to life science and even for hydrated materials samples, the effect of water should be appeared as background signal. To understand the targeted phenomena, the separation of spectra from water and sample (e.g., biosample) is necessary.

CONCLUSION

So far the muon and Mu fraction in water and ice were studied by several groups. In water, missing fraction and relaxation of Mu (based on purity of water) were understood. In ice, there is no missing fraction. It is important to know the stopping site and interaction of muon with nearby protons in water and ice which will help to separate the background signal from water in aqueous, biological and hydrated samples.

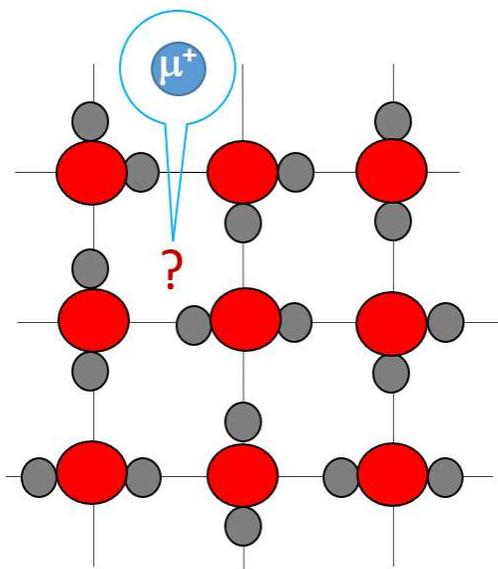


FIGURE 4. Schematic diagram (square ice) of ice following ice rules. Stopping site of muon is not understood in the system.

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REFERENCES

- Aleks Reinhardt and Bingqing Cheng. Quantum-mechanical exploration of the phase diagram of water. *Nature communications*, 12(1):1–7, 2021.
- Kanetada Nagamine. *Introductory Muon Science*. Cambridge University Press, 2007.
- Kanetada Nagamine, FL Pratt, Seiko Ohira, Isao Watanabe, Katsuhiko Ishida, Satoshi N Nakamura, and Teiichiro Matsuzaki. Intra- and inter-molecular electron transfer in cytochrome c and myoglobin observed by the muon spin relaxation method. *Physica B: Condensed Matter*, 289:631–635, 2000.
- K NAGAMINE and E TORIKAI. Electron transfer in proteins and DNA probed by muon spin relaxation. *JOURNAL OF PHYSICS: CONDENSED MATTER*, 16(40):S4797–S4806, SEP 2004.
- Paul W Percival, Hanns Fischer, Mario Camani, Fredy N Gy-gax, Walter Rüegg, Alexander Schenck, Hugo Schilling, and Heinz Graf. The detection of muonium in water. *Chemical Physics Letters*, 39(2):333–335, 1976.
- C Buci, PR Crippa, GM de’Munari, G Guidi, M Manfredi, R Tedeschi, A Vecchi, and P Podini. Interaction of muonium with molecules of biological interest in water solution. *Hyperfine Interactions*, 6(1):425–429, 1979.
- L Cristofolini, Kosmas Prassides, K Vavakis, A Amato, FN Gy-gax, A Schenck, S Gider, and DD Awschalom. A $\mu+$ sr study of the magnetic properties of ferritin. *Hyperfine Interactions*, 104(1):269–274, 1997.
- Mark TF Telling and Susan H Kilcoyne. Electron transfer in apo-ferritin probed by muon spin relaxation. *Physica B: Condensed Matter*, 374:451–455, 2006.
- Penny L Hubbard, Vasily S Oganessian, Nail Sulaimanov, Julea N Butt, and Upali A Jayasooriya. Avoided level crossing muon spectroscopy of free radicals formed by muonium addition to the constituents of dna. *The Journal of Physical Chemistry A*, 108(42):9302–9309, 2004.
- K. Nagamine, K. Shimomura, K. Imai, and J.S. Schultz. Probing magnetism in human blood by muon spin relaxation. *Physica B: Condensed Matter*, 374-375:444–447, 2006.
- Masayoshi Kobayashi, Ichiro Tanaka, Tamiko Kiyotani, and Nobuo Niimura. Towards direct observation of electron and proton transfers due to enzymatic reaction in trypsin by μ sr. In *Proceedings of the 2nd International Symposium on Science at J-PARC—Unlocking the Mysteries of Life, Matter and the Universe—*, page 033006, 2015.
- Lucia Bossoni, Laure Grand Moursel, Marjolein Bulk, Brecht G Simon, Andrew Webb, Louise van der Weerd, Martina Huber, Pietro Carretta, Alessandro Lascialfari, and Tjerk H Oosterkamp. Human-brain ferritin studied by muon spin rotation: a pilot study. *Journal of Physics: Condensed Matter*, 29(41):415801, sep 2017.
- A D Pant, K Nagamine, I Shiraki, E Torikai, K Shimomura, F L Pratt, H Ariga, K Ishida, and J S Schultz. Muonium response to oxygen content in biological aqueous solutions for cancer research. *Journal of Physics: Conference Series*, 551:012043, dec 2014.
- Amba Datt Pant, Kanetada Nagamine, Eiko Torikai, Ichiro Shiraki, Koichiro Shimomura, Francis L Pratt, Hiroko Ariga-Miwa, Katsuhiko Ishida, and Jerome S Schultz. Muonium response to low oxygen levels in haemoglobin and other biological aqueous solutions and potential application toward monitoring hypoxia. *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment*, page 165561, 2021.
- Wataru Higemoto, Ryosuke Kadono, Naritoshi Kawamura, Akihiro Koda, Kenji Kojima, Shunsuke Makimura, Shiro Matoba, Yasuhiro Miyake, Koichiro Shimomura, and Patrick Strasser. Materials and life science experimental facility at the japan proton accelerator research complex iv: The muon facility. *Quantum Beam Science*, 1(1):11, Jun 2017.
- Amba Datt Pant. Conventional to slow muon microscopy—a review. *BIBICHANA*, 17:139–145, 2020.
- Amba Datt Pant, T. Adachi, P. Strasser, Y. Ikeda, Y. Oishi, J. Nakamura, W. Higemoto, K. Shimomura, R. Kadono, Y. Miyake, and E. Torikai. Characterization and optimization of ultra slow muon beam at j-parc/muse: A simulation study. *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment*, 929:129–133, 2019.
- Alain Yaouanc and Pierre Dalmas De Reotier. *Muon spin rotation, relaxation, and resonance: applications to condensed matter*, volume 147. Oxford University Press, 2011.
- Paul W Percival, Emil Roduner, and Hanns Fischer. Radiolysis effects in muonium chemistry. *Chemical Physics*, 32(3):353–367, 1978.
- Paul W Percival. The missing fraction in water. *Hyperfine Interactions*, 8(4-6):325–328, 1981.
- DC Walker, YC Jean, and DG Fleming. Muonium atoms and intraspur processes in water. *The Journal of Chemical Physics*, 70(10):4534–4541, 1979.
- Kanetada Nagamine, Kusuo Nishiyama, Jun Imazato, Hisayoshi Nakayama, Masayuki Yoshida, Yoichi Sakai, Haruo Sato, and Takeshi Tominaga. Long-lived muonium in water revealed by pulsed muons. *Chemical Physics Letters*, 87(2):186–191, 1982.
- Emil Roduner, Philip L. W. Tregenna-Piggott, Herbert Dilger, Köbi Ehrensberger, and Masayoshi Senba. Effect of mass on particle diffusion in liquids studied by electron spin exchange and chemical reaction of muonium with oxygen in aqueous solution. *J. Chem.*

- Soc., Faraday Trans.*, 91:1935–1940, 1995.
24. SFJ Cox, JAS Smith, and MCR Symons. Measurement of 17 quadrupole interactions and identification of the diamagnetic fraction in ice by muon level crossing resonance. *Hyperfine Interactions*, 65(1):993–1003, 1991.
 25. Paul W Percival, Jean-Claude Brodovitch, Sius-Keung Leung, and Kenneth E Newman. Muonium in ice. *Hyperfine Interactions*, 18(1):543–550, 1984.
 26. Paul W Percival, Kim M Adamson-Sharpe, Jean-Claude Brodovitch, Sius-Keung Leung, and Kenneth E Newman. Partial spin depolarization of muonium in ice. *Chemical physics*, 95(2):321–330, 1985.
 27. SFJ Cox. μ sr studies of ice, illustrating the positive muon as a magnetic resonance probe of structure and dynamics. *Physica Scripta*, 1992(T45):292, 1992.
 28. SFJ Cox, N Ayres De Campos, PJ Mendes, JM Gil, A Kratzer, VM Niold, and JAS Smith. Level crossing resonance in ice: Identification of two diamagnetic muon states. *Hyperfine Interactions*, 86(1):747–752, 1994.
 29. Paul W Percival, Jean-Claude Brodovitch, Kenneth E Newman, and David P Spencer. Evidence for anisotropic diffusion of mu in ice and implications for h. *Chemical Physics Letters*, 93(4):366–370, 1982.
 30. Y Wang, SL Dong, AI Kolesnikov, P Zhang, and JC Li. Muon-spin-relaxation studies of high pressure phases of ices. *Physica B: Condensed Matter*, 350(1-3):E451–E454, 2004.
 31. Paul W Percival, Jean-Claude Brodovitch, and David M Bartels. H and mu diffusion in ice. *Hyperfine Interactions*, 85(1):91–96, 1994.
 32. Sius-Keung Leung, Jean-Claude Brodovitch, Kenneth E Newman, and Paul W Percival. Muonium diffusion in ice. *Chemical physics*, 114(3):399–409, 1987.
 33. Thomas E Markland, Scott Habershon, and David E Manolopoulos. Quantum diffusion of hydrogen and muonium atoms in liquid water and hexagonal ice. *The Journal of chemical physics*, 128(19):194506, 2008.
 34. Emil Roduner, Paul W Percival, Ping Han, and David M Bartels. Isotope and temperature effects on the hyperfine interaction of atomic hydrogen in liquid water and in ice. *The Journal of chemical physics*, 102(15):5989–5997, 1995.
 35. FG Mariam, W Beer, PR Bolton, PO Egan, CJ Gardner, VW Hughes, DC Lu, PA Souder, H Orth, J Vetter, et al. Higher precision measurement of the hfs interval of muonium and of the muon magnetic moment. In *A Festschrift In Honor Of Vernon W Hughes*, pages 229–232. World Scientific, 1992.
 36. Niels Bjerrum. Structure and properties of ice. *Science*, 115(2989):385–390, 1952.