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Journal of Nepal Physical Society
Volume 8, No 2, 2022
(Special Issue: ANPA Conference 2022)
ISSN: 2392-473X (Print), 2738-9537 (Online)

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JNPS, 8 (2), 31-36 (2022)
DOI: http://doi.org/10.3126/jnphyssoc.v8i2.50145

Published by: Nepal Physical Society
P.O. Box: 2934
Tri-Chandra Campus
Kathmandu, Nepal
Email: nps.editor@gmail.com
Crossover from Reverse Saturable to Saturable Absorptions in Two-Dimensional Tungsten Disulfide

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Abstract. The Tungsten disulfide atomic layer has enormous scientific merits that play a key role in the nonlinear absorption process. Four distinct excitonic peaks in the absorption spectra are crucial for identifying the polarity of nonlinear absorption by virtue of the resonant or non-resonant excitation process. The excitation source of 532 nm is enough for the one-photon optical transition at both low-energy excitonic peaks and two-photon transition at both higher-energy excitonic peaks. The Tungsten disulfide atomic layer exhibited the reverse saturable (or positive nonlinear) absorption through the two-step excitation process which could be possible due to the optical transition at the higher energy excitonic peaks. In addition, the polarity of the nonlinear absorption coefficient and its interchange have been analytically studied with the aid of a magnitude of excited-state absorption cross-section and Ground-state absorption cross-section. Besides, the various possible factors affecting the Z-scan results are discussed.

Received: 30 August 2022; Accepted: 14 October 2022; Published: 31 December 2022

Keywords: Atomic layer; Excitonic peaks; One-photon and two-photon excitation process.

INTRODUCTION

The nonlinear absorption (NLA) properties of the tungsten disulfide (WS\textsubscript{2}) atomic layer have emerged as an important research topic because of their optoelectronic and photonic applications [1-5]. Recently, the third-order nonlinear optical properties, which include the polarity and magnitude of NLA and nonlinear refraction (NLR) of the optical medium, have been explored extensively for both cases of inversion symmetry and asymmetry in the WS\textsubscript{2} atomic layers [2, 6]. The polarity of NLA is a prime factor for prospective technical application in optoelectronics. For example, the saturable absorption (SA) of negative nonlinearity materials are used for the lasers as Q-switching elements [7] and the reverse saturable absorption (RSA) of positive nonlinearity materials are applicable for two-photon microscopy and optical limiters [8]. Therefore, the “Z-scan technique” is used to investigate the polarity of NLA coefficient which is comparatively simple and more accurate compared to other third-order nonlinear characterization techniques [9, 10]. The WS\textsubscript{2} atomic layers have scientific merits due to the layer dependent direct/indirect band gap and their corresponding optical transition [11]. In addition, the optical spectra of WS\textsubscript{2} atomic layer show mainly four distinct absorption peaks “A”, “B”, “C”, and “D” appearing at 627, 520, 457, and 345 nm respectively as shown in Fig. 1 [5]. The layer-dependent optical transition in WS\textsubscript{2} atomic layer with specified four excitonic peaks decides the polarity of NLA through a resonant and non-resonant transition process for a given excitation energy. Therefore, the excitation source is one of the key factors affecting magnitude and polarity of NLA. The literature review revealed that the saturable absorption characteristics is prevailed via the one-photon absorption (OAP) process [1, 12]. At the same time, the RSA is observed through the two-photon absorption and/or two-step excitation due to the larger absorption cross-section in the excited state than that of the ground state [12, 13]. In the one-photon excitation process, the electric dipole transition from initial to the final state is possible due to the different parities between them. Therefore the ground-state absorption (GSA) cross-section is higher than the excited-state absorption (ESA) cross-section resulting in the dominant SA characteristics. However, in the two-photon excitation process, the electric dipole transitions...
from the initial to the final state are allowed due to the same parities between them via the different parity of an intermediate state. It implies that the excited state absorption cross-section is higher than that of the ground state, which consequences the RSA. Therefore, the excitation source at 532 nm is considered a resonant excitation source for the OPA process if only A and B excitonic peaks are considered. However, the situation might be different if C and D excitonic peaks are included in the optical transition process. It intimates that the requirements of excitation energy, in the WS$_2$ atomic layer, for the resonant and non-resonant excitation process could be rescaled if excitonic peaks at C and D are included. Neupane et al hypothesized the inclusion of excitonic peaks at C and D in the nonlinear optical transition for the first time, and then this work analytically extended the effect of the GSA and ESA on the crossover from RSA to SA and vice versa [5].

**ANALYTICAL METHOD**

The nonlinear absorption of the WS$_2$ atomic layer was analyzed by the open Z-scan technique for visible excitation source. It was a pulsed laser at 532 nm, 10 Hz repetition rate, and 6 ns temporal pulse width generated by Continuum surelite™ II-10 laser system with the beam divergence < 0.5 mrad. The open Z-scan technique characterizes the polarity and magnitude of NLA. It measures the normalized transmittance as a function of sample position moving across the focusing point of laser axis (or z-axis) using a Gaussian beam. The Gaussian beam was prepared using two-irises method [5]. The beam profiles and images were captured by a CMOS Beam Profiling Camera (USB 3.0, Edmunds). The diameter of the Gaussian beam at the focusing lens plane was 2.6 mm at FWHM of the Gaussian profile. The radius of a beam at the focal point ($w_0$) is estimated by, $w_0^2 = \frac{f}{\lambda} \frac{r}{\sqrt{1 + (\frac{r}{f})^2}}$, where $z_1 = \frac{\pi r^2}{\lambda}$, $r$ is a radius of a beam at focusing lens plane, $\lambda$ is the wavelength of a beam, and $f = 125$ mm is the effective focal length of focusing lens. The radius of beam waist at the focal point was estimated to be 15.1 µm.

The normalized nonlinear transmittance (T) with open Z-scan is given by [9],

$$T(z, S = 1) = \sum_{m=0}^{\infty} \frac{(-q)^m}{(1 + m)^{3/2}} (z_0/z)^{m},$$

for all $q < 1$ where $q(r, z, t) = \frac{1}{\alpha_0 L_{\text{eff}}} \frac{\beta I}{I_s}$ with, $I_0$ being the peak excitation intensity of input laser beam, $\beta$ is the nonlinear absorption coefficient, and $L_{\text{eff}}$ being longitudinal displacement of the sample from focus point given by $L_{\text{eff}} = \frac{1 - \exp(-x_0)}{\alpha_0 L}$. Here, $L$ is the sample thickness and $\alpha_0$ is the linear absorption coefficient. To keep the beam size constant throughout the sample, the condition for the thin sample approximation should be valid i.e., the sample thickness is much less than Rayleigh’s range $z_0 = \frac{\lambda^2}{4\alpha_0}$, where $k$ is the wave number.

The intensity dependent total absorption coefficient $\alpha(I)$ can be written in terms of incident intensity $I$, saturation intensity $I_s$, and nonlinear absorption coefficient $\beta$ as [14]

$$\alpha(I) = \frac{\alpha_0}{1 + I/I_s} + \beta I,$$
such that one can evaluate $\beta$ as

$$\beta = \frac{1}{I} \left( \alpha(I) - \frac{\alpha_0}{1 + I/I_s} \right)$$

$$= \frac{1}{I} \left( \sigma_{esa}N_{ex} - \sigma_{gsa}N_0 - \frac{\sigma_{gsa}N_0}{1 + I/I_s} \right), \quad (3)$$

where $\sigma_{gsa}$ and $\sigma_{esa}$ are GSA and ESA cross sections respectively, and $N_0$ and $N_{ex}$ are the carrier densities in the ground state and the excited state respectively. At a relatively lower excitation source, the carrier density at the excited state can be approximated by its ground state carrier density. Eq. (3) describes the contribution of absorption cross-section to distinguish the polarity of nonlinear absorption coefficient. We have used wavelength of 532 nm, laser pulse of width 6 ns, laser repetition rate of 10 Hz, beam radius of 1.12 mm at lens plane, 12.5 cm of the focal length of lens, sample length of 1 mm, and $\beta$ of magnitude $6.0 \times 10^{-8}$ m/W as fitting parameters as presented in Refs. [5, 15].

### RESULT AND DISCUSSION

The WS$_2$ atomic layer includes 1 – 4 atomic layers with lateral size of 50 – 150 nm in the ethanol and water mixture, brought from the commercial product of Graphene supermarket, which was prepared by a liquid exfoliation [16]. The absorption spectrum of WS$_2$ atomic layer is shown in Fig.1. The absorption peaks at $\sim$627 and $\sim$520 nm are assigned to the optical transitions at K-position in momentum space due to the strong spin-orbit coupling [5, 11, 17, 18]. In specific, the A ($\sim$627 nm) and B ($\sim$520 nm) absorption peaks are allocated to the transition from the highest energy level in the valence band to the lowest conduction band and from the second highest energy level in the valence band to the lowest conduction band, respectively. The excitonic peaks at $\sim$457 and $\sim$345 nm attribute to the optical transitions due to the band nesting at the region where conduction and valence bands are parallel to each other in the momentum space [19, 20].

The normalized nonlinear transmittance for the various excitation intensities as a function of the sample position $z$ is shown in Fig. 2. It exhibits the reverse saturable absorption or positive nonlinear absorption features for all given excitation intensities implying that the ESA cross section is higher than the GSA. As shown in Fig. 2, the magnitude of normalized nonlinear transmittance is decreased with an increase in the applied intensities. However, with the two highest intensities at 25.5 and 26.14 GW/cm$^2$, no further deeper valley traces are observed because of the existence of saturable absorption (SA) within an RSA [21] even in the two-step excitation process.

To the third order approximation, the transition rate $\Gamma_{if}$ from an initial state $|i\rangle$ to the final state $|f\rangle$ is given by [22]

$$\Gamma_{if} = \frac{2\pi}{\hbar} \left| \langle f | H' | i \rangle + \frac{1}{2} \sum_n \langle f | H' | n \rangle | n \rangle \langle H' | i \rangle \omega_i - \omega_h \right|^2$$

$$+ \frac{i}{\hbar^2} \sum_n \sum_m | \langle f | H' | m \rangle | m \rangle \langle H' | i \rangle | n \rangle \langle n | H' | i \rangle |^2$$

$$\times \delta(E_f - E_i - \hbar\omega), \quad (4)$$

where $E_i$ and $E_f$ are the eigenvalues of initial and final states. $\hbar\omega$ is the photon energy absorbed by the initial state to reach to the final state. The delta function $\delta(E_f - E_i - \hbar\omega)$ is nonzero only if $E_f = E_i - \hbar\omega$ is satisfied. The matrix element $\langle f | H' | i \rangle = -i e \sqrt{\frac{8\pi\varepsilon_0}{\omega_0\hbar^3}} \mathbf{r} \cdot (E_i - E_f) \langle f | \mathbf{r} | i \rangle$, represents the electric dipole transition from an initial to the final states in terms of the $\mathbf{r}$-matrix element $\langle f | \mathbf{r} | i \rangle$ [21-23]. $H'$ is the perturbed Hamiltonian due to the light-matter interaction. $E$, $\mathbf{r}$, $\omega$, $r$, $e$, and $i$ are the eigenvalues of matter, the polarization of radiation, the electronic charge of the electron, and the total time of transition, respectively. The RSA or positive nonlinearity is associated with the two-step excitation process through an intermediate state as described in Eq. (3).

The excitation source of 532 nm ($\sim$2.33 eV) is considered a resonant excitation source for the excitonic peaks at $\sim$627 nm ($\sim$1.99 eV) and $\sim$520 nm ($\sim$2.43 eV) while the non-resonant process occurs for excitonic peak at higher energies. It tells us that the one-photon excitation was located between A and B excitons, which are...
assigned to the optical transition at the K/K' valley of the first Brillouin zone. The exciton binding energy [26, 27], the difference between electronic band gap and optical band gap, of a WS\textsubscript{2} monolayer is \(\sim 0.71\) eV at K valley [28]. The large binding energy is due to the significant reduction of dielectric screening on the Coulomb interactions in the 2D atomic layer semiconductor and the tightly bounded exciton with the strong Coulomb interaction [29]. Considering the large exciton binding energy of the WS\textsubscript{2} atomic layer, the A and B excitons of the WS\textsubscript{2} atomic layers could be excited to the deep conduction band by a two-step excitation through the optical band and by two-photon excitation through the virtual state or the broad optical band, respectively. Moreover, the C (\(\sim 2.7\) eV) and D (\(\sim 3.54\) eV) excitonic peaks could be excited to the optical band or conduction band with two-photon through a virtual state. It implies that the WS\textsubscript{2} atomic layer exhibited a larger ESA cross-section than the GSA cross-section for a given excitation source which is further confirmed by Fig. 3. It displays the nonlinear transmittance as a function of sample position for a given ratio of ESA to GSA cross-section using Eqs. (2) and (3).

The color map of Fig. 3 estimated the negligible nonlinear transmittance if ESA is equal to the GSA in their magnitudes. If the ratio of ESA to GSA is larger than 1, the nonlinear transmittance results in the RSA characteristics whereas the SA features are seen for a ratio less than 1. It revealed that the WS\textsubscript{2} atomic layer has a larger magnitude of ESA than GSA, which demands the involvement of C and D excitons in the optical transition process for given excitation energy as well.

**Accuracy in Z-scan measurements**

The third-order optical nonlinearity has been investigated by a set of techniques such as Z-scan, four-wave mixing, and spatial self-phase modulation etc. in the past decade [5, 30]. These techniques are designed to characterize the different parameters associated with cubic nonlinearity because of their own limitations and advantages for different optical materials. Among them, M. Sheik-Bahae et al developed the Z-scan technique, derived from the Gaussian beam profile, to investigate the real and imaginary part of third-order susceptibility [9, 31]. It is anticipated that the failure of the required experimental setup may mislead the research finding including the polarity of the NLA. Therefore, the Z-scan experimental setup is crucial for measurement accuracy. To obtain more accurate and reproducible results, the following factors are recommended to consider while designing the Z-scan experiment [15, 32].

**a) System’s nonlinearity:** A variety of electronic and optical instruments are integrated into the Z-scan data acquisition process. Each of them has a unique polarization response to the electric field that might mislead the accuracy of the measurement. Therefore, selecting the system’s linearity range for a given laser power (or intensity) is a key step to minimize the measurement uncertainty. Fig. 4 shows the schematic graph of the transmittance beam as a function of laser peak intensity without an optical sample to display the system’s linearity ranges. It includes three different regions, namely, low intensity, moderate intensity, and high intensity, which we refer to the below 5 W/cm\textsuperscript{2}, in between 5 to 20 W/cm\textsuperscript{2}, and above 20 W/cm\textsuperscript{2}. The low-intensity region may not be enough excitation power for optical nonlinearity, the moderate intensity region shows linearity at which the experiment is suggested to conduct, and the higher intensity region is mostly saturated. In higher intensity region, the saturation limit of the detector would affect the measurement as well.

**b) Optical nonlinearity from non-sample:** The optical sample like nanoparticles, quantum dots, and two-dimensional materials are fabricated either on a suitable solid substrate or in the liquid base solution. Because of the narrow pulse and high laser power density, the transmittance measurement could include the additional polarization response to the electric field by the non-sample. It is recommended that the Z-scan experiment for only non-sample should be conducted under the same experimental condition before any measurement and then set the transmittance measurements results apart from the non-sample generated part in the experimental results [33].

**c) Sample quality:** In the Z-scan method, the beam is focused down along the z-axis which results in the variable laser power density along the laser direction. It indicates that the sample has interacted with the various laser intensity while moving along the z-axis. Inconsistency of
sample population or uneven doping in the optical sample may mislead the measurement accuracy. Therefore, it is recommended to use a high-quality sample uniformly distributed in the entire solid substrate or base solution. In specific, the concentration of the solution and the thickness of the sample pool should be uniform for the liquid-based sample. However, the sample growing method is very challenging and out of our control in some circumstances. So, the intensity scan (I-scan) technique is used to confirm the polarity of Z-scan data [34, 35].

d) Laser pointing accuracy and stability: The third-order optical nonlinearity is designed to collect the low-signal fluctuation transmittance by the detector. Therefore, it is sensitive to the power stability and its result on the measurement credibility. Stability depends on the laser quality itself, cavity instability, the current supplied, thermal effect, and many more. Therefore, two beams are designed in the Z-scan. The first beam is the reference beam that goes into the detector directly and the second beam interacts with the sample through the focusing lens before the detector. During the data analysis, the reference beam is used to normalize the nonlinear transmittance if the laser energy fluctuation is not big.

e) Thermal effect on the nonlinearity: The Z-scan technique, in general, is reliable for both pulse and CW laser sources. Also, the various laser specifications produce additional thermal mediated nonlinearity in the nonlinear transition process. It is reported that the thermal effect reorients the molecule of an optical sample or spatial alignment of atomic layers which affects the magnitude of a real coefficient of cubic susceptibility [30, 36]. To exclude the thermally induced optical nonlinearity, the repetition rate of the laser beam could be modified with a suitable chopper frequency during the measurements. But for pulse laser setup, selecting the materials having a shorter thermal diffusion time than pulse width is suitable as well.

f) Beam profile: The beam distribution in the Z-scan technique directly affects the measurements because the detector collects the spatial phase distortion of light-matter interaction. Therefore, the beam with a high-quality Gaussian beam with a single mode TEM00 beam is required for the pre-existing theoretical model. The Gaussian beam can be produced via a simple two-pin hole method [5].

g) Resolution and speed of moving sample: An adjustment of the sample moving resolution should be as small as possible. It implies that if position resolution is not small enough, we may lose the important transmittance information, especially in the valley or peak (z = 0) position. In addition, the speed of the optical sample should be uniform on the z-axis for keeping an equal interaction time between a sample and beam at each position. Therefore, the sample moving distance should be well-defined, and should not it be too big.

CONCLUSION

The polarity of NLA of the WS2 atomic layer has been studied analytically. It demonstrates the RSA characteristics for a given excitation source as it has the larger ESA than GSA cross section. The excitation source of energy \( \sim 2.33 \) eV is considered as a source for one photon excitation, which is located between A and B exciton absorption peaks. The optical transition associated with the WS2 atomic layer is the two-photon transition which simply requires the existence of C and D excitonic peaks during the nonlinear transition process. The polarity of the NLA coefficient, in terms of the magnitude of ESA and GSA, demonstrated the physical origin of crossing from RSA to SA and vice versa. In addition, the factors that might affect the results from the Z-scan method have been discussed especially for experimentalists to improve the measurement accuracy and credibility. The WS2 atomic layer with RSA phenomena has extensive technical applications in the areas of optical power limiting [37].

ACKNOWLEDGMENTS

This work is supported by the College of Arts and Sciences through funding number 101012 and Chemistry and Physics Department at The University of North Carolina at Pembroke.

EDITORS’ NOTE

This manuscript was submitted to the Association of Nepali Physicists in America (ANPA) Conference 2022 for publication in the special issue of Journal of Nepal Physical Society.

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